# Transition metal doped TiO<sub>2</sub>: physical properties and photocatalytic behaviour

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ABSTRACT. Two probe photocatalytic reactions, i.e. ethanoic acid and 4-nitrophenol photooxidation, were carried out in different experimental conditions by using suspensions of transition metal (Co, Cr, Cu, Fe, Mo, V and W) doped polycrystalline  $TiO_2$  powders in aqueous systems. A beneficial influence of the presence of metal species was observed only with the samples containing copper and tungsten. In particular, the  $TiO_2$ /Cu powders showed to be more photoactive of bare  $TiO_2$  for the ethanoic acid oxidation while the  $TiO_2$ /W samples were more efficient for 4-nitrophenol degradation. A tentative interpretation is provided on the basis of the values of the points of zero charge of the powders and of the rate constants of recombination of photogenerated electrons and holes, determined by femtosecond pump-probe diffuse reflectance spectroscopy (PP-DRS).

## 1. INTRODUCTION

 $TiO_2$  is a very suitable photocatalyst because of its optical and electronic properties, low cost, chemical stability and non-toxicity [1–3]. However, due to its bandgap energy,  $TiO_2$  utilizes only a very small fraction of the solar spectrum and thus doping with transition metals has been so far employed to extend the light absorption to the visible region [4–15].

The presence of foreign metal species is generally detrimental for the degradation of organic species but many controversial results are reported in literature. Hoffmann et al. [8] found that doping quantum-sized  $TiO_2$  with  $Fe^{3+}$ ,  $Mo^{5+}$ ,  $Ru^{3+}$ ,  $Os^{3+}$ ,  $Re^{5+}$ ,  $V^{4+}$  and  $Rh^{3+}$ at 0.1-0.5 at.% significantly enhanced the photoreactivity both for the oxidation of CHCl3 and the reduction of CCl<sub>4</sub>, while Co<sup>3+</sup> and Al<sup>3+</sup> decreased the photoreactivity. The photocatalytic activity of TiO2 toward the oxidation of 1-4 dichlorobenzene was improved significantly by the introduction of  $WO_3$  and  $MoO_3$  [10, 11] and a beneficial influence of tungsten was found for the photodegradation of 4-nitrophenol [12, 13].  $Cr^{3+}$  is reported to reduce significantly the photocatalytic performances of TiO<sub>2</sub> [5] but Cr and V ion implanted TiO<sub>2</sub> have showed photocatalytic reactivity three and four times higher than TiO<sub>2</sub> for the decomposition of NO under solar beam irradiation [16]. The method of doping obviously determines the properties of the catalyst, so that direct comparisons on the effects of metal doping require identical experimental conditions for the preparation of the samples and the use of the same bare TiO<sub>2</sub> as starting material.

The photoreactivity of the catalysts depends on several factors as for example the acid-base properties of the powders and/or the relative recombination rate of the photoexcited electrons and holes. In this work we

have tried to correlate these physical properties with the photocatalytic behaviour of polycrystalline  ${\rm TiO_2}$  powders doped with some transition metals. The activity of the samples was tested in different photocatalytic reaction systems.

## 2. MATERIALS AND METHODS

**2.1. Sample preparation.** The doped samples were prepared by the incipient wet impregnation method. The TiO2 support was obtained as follows: titanium hydroxide was precipited by reacting an aqueous solution of TiCl3 with ammonia, the white precipitate was washed repeatedly to remove residual Cl<sup>-</sup> ions, dried 24h at 373K and finally heated in air for 24h at 773 K. TiO2 was impregnated with aqueous solutions of transition metal ions ex  $Co(NO_3)_2.6H_2O$ ,  $Cr(NO_3)_3.9H_2O$ ,  $Cu(NO_3)_2.3H_2O$ , Fe(NO<sub>3</sub>)<sub>3</sub>.9H<sub>2</sub>O<sub>4</sub>, (NH<sub>4</sub>)<sub>6</sub>Mo<sub>7</sub>O<sub>24</sub>.4H<sub>2</sub>O<sub>5</sub>, NH<sub>4</sub>VO<sub>3</sub> and (NH<sub>4</sub>)<sub>6</sub>W<sub>12</sub>O<sub>39</sub>.xH<sub>2</sub>O. After standing at room temperature for 24 h, water was evaporated by heating the samples at 373 K for 24 h. The amounts of support and solution were chosen to yield solids containing 0.3, 1.0, 2.0 and 5.0 moles of dopant metal ions over 100 moles of dopant and titanium ions. The dried solids were manually ground in an agate mortar and calcined in air at 773 K for 24 h. The samples were identified by the following code: TiO<sub>2</sub>/Me/X, where Me indicates the kind of dopant metal ion and *X* its molar percentage.

The detailed characterization of these samples by means of X-ray diffraction, specific surface area measurements and scanning electron microscopy, will be published elsewhere [17].

**2.2. Point of zero charge determination.** The point of zero charge of the various powders was esti-

mated by using the method of mass titration [18] which involves finding the limiting pH value of an oxide/water slurry as the oxide mass content is increased. Varying amounts of powders were added to water and the resulting pH values were measured after 24 h of equilibration. Typical values of oxide/water by weight were 0.1, 1, 5, 10 and 20%.

- 2.3. Femtosecond pump-probe diffuse reflection spectroscopy. The relative rate constants of electron-hole recombination were estimated by using the femtosecond pump-probe diffuse reflectance spectroscopy (PP-DRS) technique whose details are described elsewhere [19].
- **2.4. Photocatalytic experiments.** The samples were employed as catalysts for two different photocatalytic reactions: (a) oxidation of ethanoic acid and (b) photodegradation of 4-nitrophenol.
- (a) 50 mg of photocatalyst were suspended with magnetic stirring in 5 ml of an aqueous solution of ethanoic acid (5 vol. %) and photoirradiated in air. Irradiation with light of wavelength  $\lambda > 300\,\mathrm{nm}$  was carried out using a 400 W high pressure Hg arc (Eikosha) through a cylindrical Pyrex glass filter and a closed glass reaction tube. Carbon dioxide was analyzed by gas chromatography.
- (b) The experiments were performed by using a cylindrical Pyrex glass reactor containing 700 mg of catalyst and 500 ml of an aqueous solution of 4-nitrophenol ( $20\,\mathrm{mg}\cdot\mathrm{L}^{-1}$ ) previously adjusted to pH 4.5. Oxygen was continuously bubbled into the stirred suspension which was irradiated by a 125 W medium pressure Hg lamp (Helios Italquartz) immersed within the photoreactor. Samples of 5 ml volume were withdrawn from the suspension at fixed intervals and, after filtration, the concentration of 4-nitrophenol was evaluated by measuring its absorption at 315 nm with a spectrophotometer Beckman DU 640.

## 3. RESULTS AND DISCUSSION

3.1. pzc measurements. The pH of an aqueous suspension of an oxide depends on the amount of powder in a given volume of water [20–22]. The point of zero charge of the oxide is the value of pH required to give zero net surface charge. The adsorption sites for anions and cations are charged surface groups resulting from the protonation-deprotonation equilibria of the surface hydroxy groups of the oxide. The knowledge of the pzc can help, in principle, to predict whether the ion exchange to a specific component of the oxide system is or not favoured.

The pzc of a composite oxide is related to the values of the pure oxide components and has values that lie between those of the two phases [23, 24]. As found by Subramanian *et al.* [23] the surface charge devel-

opment of a supported oxide is a function of dopant concentration.

According to Noh and Schwarz [18], the observation of a limiting pH value as one increases the mass fraction of solid in fresh water can be considered as an estimation of the point of zero charge of pure and composite oxides. Figure 1 shows typical plots of pH versus mass percentage of oxide for bare TiO<sub>2</sub> and the powders doped with W. The plateaus of the mass titration curves are the pH values corresponding to the pzc's of the samples. Similar curves were obtained for all the doped samples.

A decrease in pH is observed when the  $pH_{pzc}$  is lower than 7 since the surface sites tend to become negatively charged either by adsorbing  $OH^-$  ions or by desorbing  $H^+$  ions. On the contrary, an increase in pH occurs if the  $pH_{pzc}$  is higher than 7 since in this case the solid surface will be positevely charged.

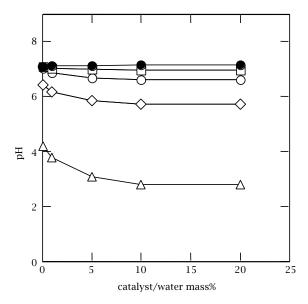


Figure 1. (a) Plot of pH versus the catalyst/water mass percentage for  $TiO_2$  and various  $TiO_2/W$  samples: ( TiO2, U TiO2/W/0.3, U TiO2/W/1.0, U TiO2/W/2.0, U TiO2/W/5.0.

The pzc values have been plotted against the content of dopant. As shown in Figure 2, the pzc of Cr, Mo, V and W-doped  $TiO_2$  moves to a lower pH as the content of metal increases, whilst for Co, Cu and Fe-doped  $TiO_2$ , the pzc moves to a value more basic than that of the bare  $TiO_2$ . The points of zero charge of the various powders are also reported in Table 1.

The pzc's of the samples containing Mo, V and W significantly decrease with increasing the metal content indicating a surface enrichment of species with an acid behaviour as  $MoO_3$ ,  $V_2O_5$  or  $WO_3$ . For the Crdoped samples, 0.3 at. % of metal is sufficient to modify strongly the pzc of  $TiO_2$  from 7.1 to 3.6 suggesting the

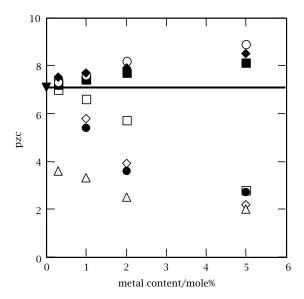


Figure 2. (b) Points of zero charge of the doped samples versus the amount of metal content (%): ( $\blacktriangledown$ ) TiO<sub>2</sub>, ( $\spadesuit$ ) TiO<sub>2</sub>/Co, ( $\triangle$ ) TiO<sub>2</sub>/Cr, ( $\bigcirc$ ) TiO<sub>2</sub>/Cu, ( $\blacksquare$ ) TiO<sub>2</sub>/Fe, ( $\diamondsuit$ ) TiO<sub>2</sub>/Mo, ( $\spadesuit$ ) TiO<sub>2</sub>/V, ( $\square$ ) TiO<sub>2</sub>/W.

presence of  $CrO_3$  on the suface of the support, as already found in previous studies [25].

*3.2.* Femtosecond pump-probe diffuse reflectance spectroscopy. Femtosecond (PP-DRS) measurements were carried out on bare and metal doped TiO<sub>2</sub> powders to obtain the rate constants of recombination of photoexcited electrons and holes.

A pump beam of wavelength at  $310 \,\mathrm{nm}$  induces a very rapid ( $< ca. 250 \,\mathrm{fs}$ ) rise of absorption at  $620 \,\mathrm{nm}$  followed by a gradual decay [26]. The rapid rise is thought to be due to the capture of photoexcited electrons at a trapping site and their recombination with holes induces the decay of the absorption in the time region of several hundreds ps. The decay profiles can be simulated on the assumption of a second order kinetics of electron-hole recombination [19].

All the undoped and doped  ${\rm TiO_2}$  powders showed similar decay profiles and by analyzing the decay curves of the various samples it was possible to estimate the rate constants of charge recombination,  $k_{\rm r}$  (cm<sup>3</sup> ps<sup>-1</sup>), which are listed in Table 1. The  $k_{\rm r}$  values of some samples containing 5% of metal are not reported because the measurements were not accurate and reproducible due to the deep colours of the powders [26]. It is clear from Table 1 that metal loading enhances the recombination of the photogenerated electrons and holes. By increasing the metal content,  $k_{\rm r}$  increases for each loaded metal with the exception of the samples containing copper or tungsten which reveal  $k_{\rm r}$  values practically constant and almost independent on the amount of metal.

Table 1. Points of zero charge (pzc) and rate constants of electron-hole recombination ( $k_{\rm r}$ ) of bare and transition metal loaded TiO<sub>2</sub>.

Sample	pzc (pH)	$k_{\rm r}~({\rm cm}^3\cdot{\rm ps}^{-1})$
TiO <sub>2</sub>	7.1	1.4
TiO <sub>2</sub> /Co/0.3	7.5	2.3
$TiO_2/Co/1.0$	7.7	2.5
$TiO_2/Co/2.0$	7.9	3.0
$TiO_2/Co/5.0$	8.5	-
TiO <sub>2</sub> /Cr/0.3	3.6	2.8
$TiO_2/Cr/1.0$	3.3	2.3
$TiO_2/Cr/2.0$	2.5	3.4
$TiO_2/Cr/5.0$	2.0	-
TiO <sub>2</sub> /Cu/0.3	7.3	2.2
$TiO_2/Cu/1.0$	7.6	2.3
$TiO_2/Cu/2.0$	8.2	2.5
TiO <sub>2</sub> /Cu/5.0	8.9	-
TiO <sub>2</sub> /Fe/0.3	7.2	2.6
$TiO_2/Fe/1.0$	7.4	4.1
$TiO_2/Fe/2.0$	7.7	4.6
$TiO_2/Fe/5.0$	8.1	4.8
TiO <sub>2</sub> /Mo/0.3	7.4	1.8
$TiO_2/Mo/1.0$	5.8	2.1
$TiO_2/Mo/2.0$	3.9	5.2
$TiO_2/Mo/5.0$	2.2	-
TiO <sub>2</sub> /V/0.3	7.4	1.9
$TiO_2/V/1.0$	5.4	3.1
$TiO_2/V/2.0$	3.6	3.7
$TiO_2/V/5.0$	2.7	-
TiO <sub>2</sub> /W/0.3	7.0	2.3
$TiO_2/W/1.0$	6.6	1.9
$TiO_2/W/2.0$	5.7	2.3
TiO <sub>2</sub> /W/5.0	2.8	2.2

3.3. Effect of the transition-metal loading on the photocatalytic activity. Figure 3(a) shows the rate of formation of  $CO_2$  as a function of the transition metal content. The rate of  $CO_2$  evolution was determined during the photooxidation of ethanoic acid from the slope of the plots relative to the amount of product vs. irradiation time by considering the initial 1.5 h of irradiation. Instead, Figure 3(b) shows the initial zero order reaction rates of the apparent kinetics of disappearance of 4-nitrophenol obtained from the curves relative to the substrate concentration vs. reaction time. For both reactions, loading of any kind of transition metal generally gives rise to a decrease in the photocatalytic activity and this effect is more significant as the amount of loaded metal increases.

The photoreactivity results indicate that the  $TiO_2/Cu$  samples are always more active than the corresponding bare  $TiO_2$  for the oxidation of ethanoic acid. The rate of  $CO_2$  evolution increases by increasing the copper content up to 1% and reaches values not much lower than the maximum for higher loading. A possible explanation is that loaded Cu is reduced into a metallic state ( $Cu^0$ ) to act as a co-catalyst, increasing

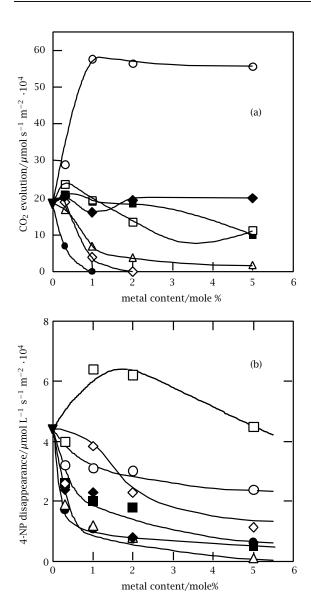


Figure 3. Rates of CO<sub>2</sub> evolution (a) and of 4-nitrophenol (4-NP) disappearance (b) versus the amount of metal content (%). Symbols as in Figure 2.

the photocatalytic activity of the support [26]. This hypothesis can be justified by the redox potential of  $Cu^+/Cu$  (+0.1 V vs. SCE) which is more positive than the conduction band of  $TiO_2$ . Moreover the colour of the  $TiO_2/Cu$  suspensions in aqueous ethanoic acid turned from ivory to black during the photoirradiation.

As for the 4-nitrophenol photodegradation, the activity of  $\text{TiO}_2/\text{W}/0.3$  is slightly lower than that of  $\text{TiO}_2$  while the reaction rates of the other  $\text{TiO}_2/\text{W}$  samples are higher than that of the support with a maximum for  $\text{TiO}_2/\text{W}/1$ . The beneficial effect of tungsten on the photoactivity of  $\text{TiO}_2$  has been explained by the formation of  $\text{W}^{5+}$  species by means of transfer of photoproduced electrons from  $\text{TiO}_2$  to  $\text{W}^{6+}$ . Subsequently  $\text{W}^{5+}$ 

oxidises to  $W^{6+}$  by transferring electrons to adsorbed  $O_2$  [10, 12].

The observed different behaviour exhibited by the  ${\rm TiO_2/Cu}$  samples when they are used to photodegrade ethanoic acid and 4-nitrophenol could be explained by taking into account that the formation of  ${\rm Cu^0}$  is greatly favoured for high concentrations of organic molecules, acting as hole traps. It is worth noting that the runs for 4-nitrophenol degradation were carried out with a very low initial concentration of this organic substrate. Moreover, the pzc's of the  ${\rm TiO_2/Cu}$  samples (see Table 1) are quite basic so that the interaction between surface of the catalyst and ethanoic acid (an acid stronger than 4-nitrophenol) is favoured. On the contrary, the interaction with 4-nitrophenol could be more important for the  ${\rm TiO_2/W}$  samples whose pzc values are rather acid.

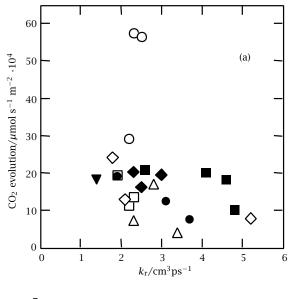
It is not easy to rationalize the low efficiencies obtained in the presence of all the other dopants as many physicochemical and/or intrinsic electronic factors can influence beneficially or detrimentally the photocatalytic activity of the doped TiO<sub>2</sub> powderds [17].

3.4. Dependence of the photocatalytic activity on  $k_{\rm r}$ . The lifetime of trapped electrons has been related to the photocatalytic activity of bare and metalloaded  ${\rm TiO_2}$  powders [19]. As a general trend, the longer the lifetime of trapped electrons, the higher the photocatalytic activity of the samples.

Figure 4 shows the correlation between the rates of the reactions (a) and (b) and the values of  $k_{\rm r}$  of the various samples, reported in Table 1. For the oxidation of ethanoic acid (Figure 4(a)), the relation between photoactivity and electron-hole recombination rate is rather confusing due to the high photoefficiencies of the TiO<sub>2</sub>/Cu samples whose  $k_{\rm r}$  values are also quite similar each other. By removing the results of these samples from the figure, the reaction rate of CO<sub>2</sub> production appears to be almost indipendent of  $k_{\rm r}$ .

According to a simple kinetic model [26], it is expected that the e<sup>-</sup>-h<sup>+</sup> recombination is detrimental to the photocatalytic activity unless the photogenerated pairs react efficiently with the surface adsorbed substrates. If the decomposition of ethanoic acid is carried out under an Ar atmosphere [26], a  $k_r$  dependence similar to that of reaction (b) is obtained, indicating that the presence of O2 makes negligible the influence of the electron-hole recombination. By presuming that the reaction proceeds via oxidation of surface adsorbed etanoic acid by h<sup>+</sup> and reduction of O<sub>2</sub> by e<sup>-</sup>, probably the rate of  $CO_2$  evolution does not depend on  $k_r$  because, in the presence of air, the surface-adsorbed O2 reacts with e<sup>-</sup> before its recombination. Obviously, it cannot be excluded that many other factors control the rate of the reaction.

The plot of Figure 4(b) is fairly scattered but it can be noticed that, with increasing  $k_r$ , the rate of 4-



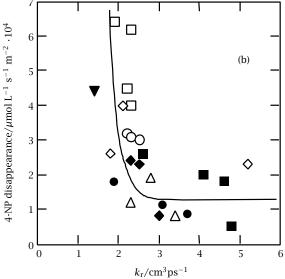


Figure 4. Relation between  $k_{\rm r}$  values and the rates of  ${\rm CO_2}$  evolution (a) and of 4-nitrophenol (4-NP) disappearance (b). Symbols as in Figure 2.

nitrophenol disappearance first significantly decreases and then becomes practically constant. By assuming that the photoactivity of the samples is inversely proportional to the increase in  $k_{\rm r}$  [26], this means that the net activity of 4-nitrophenol photodegradation is dominated by the electron-hole recombination rate when the  $k_{\rm r}$  values are relatively low whereas the reaction rate becomes indipendent of  $k_{\rm r}$  when the recombination of the photogenerated pairs is too fast.

An explanation for the two different  $k_r$  dependences can be based on the assumption that the distance between the place where  $e^-$ - $h^+$  pairs form and react with the substrates depends on the type of photoreaction [26]. The reaction of 4-nitrophenol degradation proceeds through several steps and numerous intermediates so that oxidation and reduction by  $h^+$  and  $e^-$  likely occur at separate sites. It seems reasonable to infer that the rate of the reaction depends on  $k_{\rm r}$  since  $e^-$  (or  $h^+$ ) must migrate in the bulk or on the surface of the catalyst particles. Instead, the oxidation of ethanoic acid and the reduction of  $O_2$  occur at neighbouring sites so that the scarce dependence of the rate of  $CO_2$  evolution on  $k_{\rm r}$  could be justified by a negligible migration of  $e^-$  (or  $h^+$ ).

The different relations between  $k_{\rm r}$  values of the various samples and the rates of the reactions (a) and (b) can be also due to the different experimental conditions under which the reactions (a) and (b) were carried out. In fact, ethanoic acid, due to its high concentration, can work as an efficient hole trap, levelling the influence of the recombination rates of the various powders.

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