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### Research Article

## An Efficient Deployment Model for Maximizing Coverage of Heterogeneous Wireless Sensor Network Based on Harmony Search Algorithm

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Due to the increase of Wireless Sensor Network (WSN) technologies demand, the optimal sensor node deployment is considered as one of the most important factors that directly affect the network coverage. Most researches in WSNs that solved the problem of coverage in homogeneous and heterogeneous cases are suffering from many drawbacks such as consumed energy and high cost. In this paper, we propose an efficient deployment model based on probabilistic sensing model (PSM) and harmony search algorithm (HSA) to achieve the balance between the network coverage performance and the network cost in a heterogeneous wireless sensor network (HEWSN). The HSA is used for deployment optimization of HEWSN nodes which makes a balance between the coverage and financial cost. The PSM is used to solve the overlapping problem among the sensors. The performance of the proposed model is analyzed in terms of coverage ratio and cost evaluations. The simulation results showed the capability of the proposed heterogeneous deployment model to achieve maximum coverage and a minimum number of sensors compared to homogeneous deployment. Furthermore, a comparative study with a meta-heuristic genetic-based algorithm in HEWSN has also been conducted, and its results confirm the superiority of the proposed model.

#### 1. Introduction

Over the past decade, wireless sensor networks (WSNs) have become a wealthy research field, providing several new trends of applications. Nowadays, WSNs are considered an integral part of the Internet of Things (IoT) systems [1]. WSNs are set of low-power, low-cost, small size, and multifunctional sensor nodes that work together to sense the field, perform data processing, and communicate over AoI wirelessly. Nodes send the data aggregation to a specific station called sink or data sink, which is used to send information outside WSN to the end-user as shown in Figure 1 [2].

Current applications of WSNs include the applications that use WSN in physical life, such as military, civilian, connected vehicles, smart cities, smart grids, smart healthcare, networks of robots, and disaster recovery network civilian. For example, in the military, the WSN is used for targeting system and battle-field surveillance. In the civilian application, WSN can monitor building, traffic, environment, wildlife, security, smart agriculture system, and several other applications [3, 4]. The design of several WSN applications requires deciding an exact place of the optimal positions of sensor nodes to be located in AoI [5].

Maximizing the coverage area of the WSN system has been a current research area of WSN in the last years. Actually, WSN depends upon coverage of the network that is basically depending upon the deployment of sensor nodes [6]. The coverage area has several types based on the observed field such as the barrier coverage (means how can to protect the area from an intruder), point coverage (means how to cover a group of points), and full coverage (means that every

point in the AoI is covered by at least one sensor). In each coverage type, the quality of each point can be assessed after the deployment process [7, 8].

The deployment problem of WSN is a critical issue because it affects both the overall performance and the energy consumed by the sensors in the whole system [9, 10]. The deployment scheme is constructed according to many factors such as application, kind of sensor, and environment of the sensor [11]. Sensors can be deployed in AoI either deterministically, i.e., planned or randomly [12]. The planned sensor deployment is applied in many studies. For example, Authors in [10] proposed a novel algorithm in planned deployment was called maximal coverage hybrid search algorithm to achieve maximum coverage with a minimum number of deployment sensors. However, this type can be used for the placement of sensor nodes in the small-scale area and is not practical to cover AoI such as hostile environments and large regions. The second type of WSN deployment is called random sensor deployment, which is the most popular deployment strategy and can be considered in this paper. Dynamic deployment was used to enhance coverage in WSNs by redistribution sensor nodes after initial random deployment [13]. In the same view, for the sensor localization, a novel localization methods using dynamic deployment, collection of a novel local search process, and HS algorithm was used in [14].

Further, the deployment states are divided into four states: predeployment, initial deployment, postdeployment, and redeployment. The predeployment and initial deployment are using the manual placement of the nodes by a human or a robot or launching them from a plane. The redeployment was used in adding new nodes to the network to replace some broken. A postdeployment phase is used when the network topology has been evolved due to a relocation of nodes [15, 16]. According to the density, a sensor network deployment could be a sparse or dense deployment in which low or high number of sensors is used to cover AoI, respectively. The sparse deployment type is used when obtaining maximum coverage using less number of nodes. The dense sensor deployment type usually has more number of nodes in the AoI than required [17].

In general, WSN environments can be categorized as heterogeneous or homogeneous wireless sensor nodes. The homogenous wireless sensor nodes include sensors that have the same sensing range, communication range, and the same energy. The networks having the sensors which have various sensing range, communication range, network protocols, or different power are named heterogeneous sensor nodes. Heterogeneous sensor deployment has many features, such as it can obtain a more effective and flexible network. Also, it can increase network performance and takes into account reducing the cost of sensor deployment, energy, and communication [7, 18–20].

Maximum coverage sensor deployment problem presented with different exact and meta-heuristic algorithms. The meta-heuristics are most widely used. The harmony search algorithm is a recent meta-heuristic algorithm which was invented by [21]. HSA has successfully applied to solve a wide range of NP-complete optimization problems [22]. It is

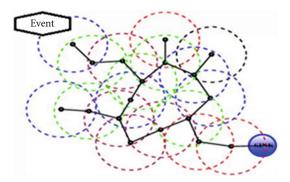


FIGURE 1: A general architecture for WSN.

inspired by the natural musical performance procedures that occur when a musician searches for a better state of harmony. According to [23], HSA has many features in comparison with traditional optimization techniques can be summarized as follows:

- (i) Fewer mathematical requirements (low amount of computation), free divergence
- (ii) HSA may overcome the limitation of GA by considering the relationship among all decision variables, whereas the GA only considers the relationship of only two parents in each enhancement

Therefore, HSA in HEWSN will be a good alternative to solve the coverage problem. Moreover, it can make a balance between maximizing the coverage and reduction of both financial cost and unnecessary energy consumption.

The optimization of random deployment problem is the critical issue in WSN applications that required the optimization of maximum coverage with minimum deployment cost. The optimization problem for coverage is related to power saving, network reconfiguration, and cost-minimizing. The deployment cost of the sensing nodes is the major factor in WSNs. WSN is a combination of many sensors where's each sensor node has a limited radion range. Thus, the researcers in [24] studied the optimum numbers of sensors that can reduce the network cost and maximize the coverage efficiently.? Although maximum coverage sensor deployment with minimum cost in WSNs has often been investigated in many studies [20], the performance of coverage is still unbalanced and suffering from many drawbacks such as energy and financial cost. In addition, research on this problem in HEWSN has progressed at a slow pace. In several WSN applications, the constructed nodes are provided with many types of sensors to provide various sensing services which can be achieved by heterogeneous sensors only [25]. Moreover, using an optimal mixture of some inexpensive low capability devices and some expensive high-capability devices can significantly enhance the performance and coverage and extend the duration of a network's lifetime [20, 26, 27].

In this paper, we consider the problem of maximizing coverage area in heterogeneous WSN with an optimized sensor deployment and minimization in sensors overlapping. The main contribution of this paper is summarized as:

(1) We propose an efficient deployment model in HEWSN which gives a maximum coverage area with the optimized number of sensor nodes (network cost)

- (2) In this model, we develop the PSM of the homogenous WSN in [11] to minimize the overlapping problem in HEWSN and explore the ability of the modified HS algorithm in providing solutions for HEWSN coverage problems in a way that the optimal deployment sensor nodes such that the network cost can be minimized and the coverage requirements can be satisfied
- (3) A modified objective function based on HEWSN combines coverage ratio, the number of sensor nodes with different sensing range, and the minimum distance between sensor nodes is proposed to support the selection of the optimal number of sensor nodes and their locations
- (4) This model which consists of PSM and HS algorithm is the first that was used in HEWSN deployment, and the comparative study is conducted with a homogeneous deployment using HS algorithm and a metaheuristic genetic-based algorithm in HEWSN using different performance analysis including maximum coverage, network cost, and overlapping effect

The rest of the paper is organized as follows. Section 2 introduces the literature reviews. The proposed HEWSN deployment model and problem definition are described in detail in Section 3. In Section 4, the experimental results and comparative study with those of other state-of-the-art methods are explained in detail. The conclusions of this study are presented in Section 5.

#### 2. Literature Review

The research works classified the deployment environment to HEWSN and HOWSN deployments. Actually, most studies in WSNs have focused on the deployment of many numbers of inexpensive homogenous sensor devices. However, in practical settings, it is often suitable to consider HEWSN deployment that has various capabilities [26]. HEWSN deployment takes into account the reducing costs of sensor deployment, energy, and communication. In addition, HEWSN deployment can be covered in a broad area and can be more efficient than HOWSN deployment. Authors in [28] tested the complete coverage problem of circular sensing footprints through various radii by two configurations of heterogeneous. In the first case, the best results are obtained when the sensing radius for one kind of nodes is approximately half of the others. The second case, including sensing cost and optimum coverage density, is obtained when the sensing radius of one disk is almost about onefifth of the other. The results showed that more efficient coverage can be obtained, and the sensing cost is significantly minimized of HEWSN deployment as compared to the HOWSN deployment case. HEWSN deployment acts also a role in improving the network's lifetime and coverage of WSN by extending the network life cycle. The optimal HEWSN deployment can extend lifetime sensing coverage by many times as much as with HOWSN deployment. It takes into account both the initial coverage and the duration of sensing operation [29]. Authors in [30] introduced mathematical models to study the effect of HEWSN deployment on the network's coverage and energy consumption using sensors of different types. The simulation results showed maximizing coverage and energy consumption. In addition, HEWSN deployment was also used for increasing network security [31]. The authors introduced reinforced barrier-coverage with consideration of HEWSN deployment in various capabilities. It used this tool to guarantee that any penetration variation of the intruder is monitored by at least one sensor and to extend the lifetime of heterogeneous reinforced barriers.

In contrast, there is another kind of sensor called smart nodes. Smart nodes are deployed according to the distance information to maximize the coverage and the network connectivity. Authors in [32] introduced smart nodes to provide the link establishment between unconnected nodes and the sink. Simulation results proved that the coverage would be increased with a limited minimum optimum number of heterogeneous smart nodes and connectivity. Still, the smart nodes have some limitations such as an expensive cost.

In HEWSN, authors in [33] used heterogonous sensor deployment to solve the obstacles of the WSN coverage problem. They proposed a novel algorithm based on the circle packing technique. They have confirmed that the proposed algorithm avoided the obstacle, produced sensor deployments of broad coverage, and minimized the sensing range demanded for each inside sensing node for accomplishing the packing condition. Authors in [34] used GA to maximize the coverage in the heterogeneous case by removing intersection among the nodes. Experimental results showed that no intersection between the nodes and the coverage area was maximized. Authors in [35] presented PSM and an improved GA (IGA) to maximize the coverage with a number of sensors which have different sensing ranges. In addition, the definition of the overlapping for the fitness function includes in these improvements. The algorithm tested on 15 states was constructed for this problem. The simulation results showed that the proposed algorithm is effective in all terms of the computational complexity, stability, and quality of solutions. However, this improved version of GA is still suffering from high complexity, because of using many sensors with various sensing radius.

The Particle Swarm Optimization (PSO) algorithm has been applied to solve optimization problems in WSNs [20]. Authors in [36] proposed an energy-efficient and light-weight self-organized distributed greedy heuristic algorithm to maximize coverage area with a minimal number of mobile nodes. They used random deployment of nodes with sufficient node density over two-dimension areas. Simulation results showed the improved performance of the proposed technique in terms of average displacement of nodes, the number of computation rounds, and the number of active nodes. In HEWSN, Song et al. [37] proposed a distributed coverage control law with mobile sensors and PSM based on PSO. The methodology was used to minimize

the coverage cost, as well as communication ranges, and exceed a threshold. However, they discarded the connectivity process. In fact, PSO has a high-quality solution, simplicity, and fast convergence. On the other hand, PSO has some limitations, such as using big amounts of memory which may limit its implementation to base stations [38].

Ant Colony Optimization (ACO) provided solutions to problems in HEWSN, such as [39]. The authors proposed a swarm intelligence based on the ACO method. The methodology depended on searching the maximum number of connected covers that achieve both sensing coverage and network connectivity. Simulation results showed that the proposed method provided a more approximate, effective, and efficient way for extending the lifetime of HEWSN. In the same context, Lin et al. [40] proposed an ACO technique that can maximize the lifetime of HEWSN. This technique depended on searching the maximum number of disjointassociated covers that satisfy both network connectivity and sensing coverage. Simulation results approved the effectiveness and efficiency of the technique and showed that an ACO is a promising method for extending the HEWSN lifetime.

Harmony search algorithm (HSA) is a music-based meta-heuristic algorithm for solving optimization problems. This algorithm has been proposed to solve several kinds of problems in the previous decade, generating very effective and efficient results in WSN. For the coverage problem in HEWSN, the HS algorithm is not used yet for deployment optimization in HEWSN, but is used in HOWSN in several researches. It is more efficient compared to other metaheuristic algorithms and traditional techniques that computationally expensive [23]. HSA is selected to maximize the coverage and minimize the number of deployed sensors in WSN. HSA had many providing solutions for WSN problems. For solving coverage and connectivity, Halim et al. [41] implemented modified HSA for node deployment purpose and enhancing the coverage. The modified HSA outperformed better compared to HSA such as the highest coverage achieved by modified HSA is 70% while HSA highest coverage is 54%. However, it suffers from high energy cost, and the full coverage is still unreachable. Mohamed et al. [42] examined a scalable HSA in terms of k-coverage enhancement algorithm and execution time. The proposed algorithm tried to improve initial coverage and to achieve the required K -coverage degree efficiently. Also, the same author in [13] proposed HSA based on dynamic deployment to maximize the network coverage and connectivity. Authors in [43] have proposed the combination of the Markov chain model and HSA to solve the coverage hole problem by redistribution mobile nodes after the initial deployment of the static nodes. The HSA was applied to set the optimal positions of the added mobile nodes, and the Markov chain model was applied to illustrate the network schemes. Authors in [44] also proposed HSA to enhance the connectivity of the nonuniform density WSNs. The simulation results showed an increased coverage area of the cluster nodes and network connectivity significantly.

Maximizing network lifetime and minimizing energy consumption is another problem solved by HSA in WSN.

Authors in [45] proposed a proper position for the date sink node that gathers data from whole sensors. Also, they proposed two phases in WSN using the improved HSA; the first phase is used to achieve a sensor node deployment by making the sensors power balanced in both k-coverage and connected WSN. The second phase tries to increase the network lifetime by moving a few of high power consumption mobile nodes to the nearest locations of low power consumption ones. Authors in [46] introduced a protocol built on HSA to cover all of the target areas by adjusting the sensing range of every sensor node. The results showed decreasing both the nodes sensing radius and energy consumption. Authors in [47] introduced both HSA and topology control protocol. This protocol has many tasks such as learning automata to set the suitable transition radius of the sensor nodes in a distributed topology environment. In addition, it is able to supply the full connectivity in sparse deployment and to extend the lifetime of the sensor network by keeping the energy consumption least. The simulation results showed the efficiency of the proposed protocol. Authors in [48] proposed a new algorithm that is named efficient energy dynamic clustering based on HSA that orders the network sensors into a suitable number of clusters. Simulation results showed that the proposed algorithm could achieve an optimal number of clusters in each round during simulation. Authors in [49] proposed combining HSA with ACO to improve the performance of each other. The role of modified HSA is to increase the network lifetime. Authors in [50] proposed an enhanced HSA in a k-covered and connected WSN. The objective is to achieve optimal coverage with sensor node deployment and efficient energy by staying node k-coverage and connectivity in hotspot areas. On the same idea, Authors in [51] examined HSA to display a solution of the coverage area targets with at least both energy consumption and *k*-sensors in the systems and compare its results with the PSO algorithm. Simulation results appeared that the HSA had more control either in minimizing the whole of sensor turns or in accomplishing k-coverage and higher convergence rate than PSO. Authors in [52] proposed a shared-infrastructure deployment problem technique to maximize the coverage network, and HSA is adjusted and assigned maximum budget to introduce a solution for metropolitan WSNs. Authors in [53] proposed an HSA for choosing the optimal path in WSN to achieve objective optimization such as reducing the transmitted power consumption and the network transmission delay. An improved particle swarm optimization (PSO) combined with a mutation operator is introduced to search the parking positions with optimal coverage rate. Then, the genetic algorithm (GA) is adopted to schedule the moving trajectory for multiple mobile sinks [54].

For minimizing cost, Wang et al. [55] introduced a model called binary differential evolution harmony search to achieve many factors such as minimum cost, reliability, and scalability of industrial WSNs. The simulation results demonstrated that the improved model is efficiently valid and reliable. Authors in [11] proposed an HSA and compared their results to GA. The simulation results showed the superiority of HSA on GA for maximizing the network coverage and minimizing the number of sensor deployment by a factor

of 40%. However, it has a higher cost compared to HEWSN. Sun et al. [56] minimized cost by determining the positions of the base station, sensor nodes, and relay nodes in both single-tiered and two-tiered to meet the coverage and connectivity requirements.

Look closer to what has been so far presented in the previous studies, we find most studies in WSNs that solved the problem of coverage in homogeneous case are still suffering from many drawbacks such as high consumed energy and high financial network cost. Furthermore, and another look at the other meta-heuristic-based solutions for HEWSN presented in this section, none of them addresses the problem of finding the optimal number of sensor nodes that can minimize the network cost and at the same time maximize the network coverage. The HS-based solutions were providing optimum solutions to different problems in HOWSN, but were not included in HEWSN coverage problems. Encouraged by these finding, the proposed work requires a more balancer method between maximizing coverage and reducing unnecessary network cost with an overlapping minimization, therefore we propose a solution in HEWSN for finding the optimal number of sensor nodes (i.e., the network cost) in a way that the optimal location of these sensors can be reached (i.e., full coverage) using PSM and HS algorithm. (a) According to the three parameters of HSA, Harmony Memory Considering Rate (HMCR), Pitch Adjusting Rate (PAR), and Bandwidth (BW<sub>range</sub>), the HSA can find the suitable number of sensor nodes as well as its positions. In addition, PSM can solve the overlapping problem.

A description of the proposed model and the problem formulation that is considered in this research is presented in the next section.

#### 3. HEWSN Deployment Model and Problem Formulation

This section presents the block diagram of the proposed HEWSN deployment model, which is divided into four main steps. The first step overviews the general assumptions and preliminaries of the AoI initialization in subsection A. In the second step, the methodology of HEWSN random deployment is presented in subsection B. In the third step, the determination of coverage probability based on PSM is introduced in subsection C. In the last step, the HSA which is considered the optimization algorithm is presented in subsection D. Figure 2 shows the block diagram of the proposed model.

- 3.1. Assumptions and Preliminaries of AoI. The assumption and preliminaries of AoI are presented as follows:
  - (i) The AoI has 2-D, width (W), and height (H).
  - (ii) Two types of nodes with different sensing ranges  $R_{s_i}$  which represent the radius of each sensor node as given in the following equation:

$$R_{s_i} = f_i \left( \frac{\text{sensing\_range}}{i} \right) \quad i = 1 \text{ to } n,$$
 (1)

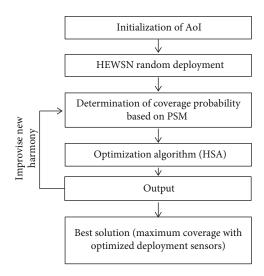


FIGURE 2: The block diagram of the proposed model.

where  $f_i$  is the number of different sensing ranges types (i.e., if sensing range = 10 meter,  $R_{s_1} = 10$  meter,  $R_{s_2} = 5$  meter,....etc.).

Uncertainty range represents uncertainty value in the coverage sensor detection. We assume that its value equal to half of  $R_s$  [57] and is given in the following equation

$$U_e = \frac{R_{s_i}}{2}. (2)$$

- (i) The AoI divided into a number of rows and columns which are represented in a group of cells
- (ii) According to [58, 59], each cell size has the same dimensions and is set manually based on the sensor's sensing range. The number of cells in width and height of AoI is calculated according to the following equations, respectively

$$Cells_{W\_Dim} = \left| \frac{W}{cell \text{ width}} \right|$$
 (3)

$$Cells_{H_{Dim}} = \left| \frac{H}{cell\_height} \right|$$
 (4)

(iii) Nodes are immobile, i.e., static

The target point is the center of each cell which located at  $x_{th}$  row and  $y_{th}$  column as illustrated in Figure 3.

#### 3.2. Problem Formulation

3.2.1. HEWSN Random Deployment. The maximum number of deployed sensors is equal to the AoI cells. Each sensor node position in AoI encodes in real number. Each position

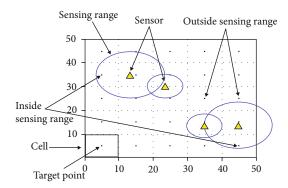


FIGURE 3: Set of target points in the area of interest  $50 \times 50 \text{ m}^2$ .

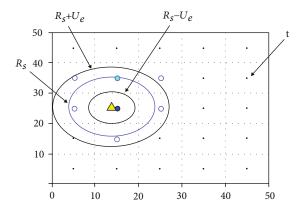


FIGURE 4: An explanation of probabilistic sensing model.

represents both x-axis and y-axis, which is determined under consideration of the lower and upper boundaries for each sensing node. The lower boundaries of each sensor node are shown in the following equations, respectively [11].

$$lower_{xsi} = R_{s_i} - U_e,$$

$$lower_{ysi} = R_{s_i} - U_e,$$
(5)

where the lower<sub>xsi</sub> and lower<sub>ysi</sub> are lower boundaries of x-axis and y-axis for every sensor node. The upper boundaries of each sensor node are defined in the following equations, respectively:

$$upper_{xsi} = W - (R_{s_i} - U_e), \tag{6}$$

$$upper_{y_{si}} = H - (R_{s_i} - U_e), \tag{7}$$

where W and H are the dimensions of AoI, whereas upper  $_{x_{si}}$  and upper  $_{y_{si}}$  are upper boundaries of x-axis and y-axis for every sensor node. The aim of boundaries calculation in both Equations (6) and (7) is to avoid sensing unnecessary field by preventing sensor nodes from being close to the sensing field border, which leads to save up energy.

In this paper, the deployment process is done randomly. So, the random positions for each sensor node are produced in the following equations.

$$xs_i = lower_{xsi} + (upper_{xsi} - lower_{xsi}) \times rand()$$
 (8)

$$ys_i = lower_{y_{si}} + \left(upper_{y_{si}} - lower_{y_{si}}\right) \times rand\left(\right)$$
 (9)

where rand () is a random function used to generate numbers within (0, 1). However, Equations (8) and (9) are used to generate unlimited random positions. Therefore, we assume a restricted range between the minimum and the maximum number of sensors as illustrated in the following equations [11]:

Min\_no<sub>S</sub> = 
$$\frac{W}{2(R_{s_i} + U_e)} \times \frac{H}{2(R_{s_i} + U_e)}$$
, (10)

Max \_no<sub>S</sub> = 
$$\frac{W}{2(R_{s_i} - U_e)} \times \frac{H}{2(R_{s_i} - U_e)}$$
, (11)

where  $R_{s_i}$  is the sensing range,  $U_e$  is the uncertainty range, and both were calculated in Equations (1) and (2), respectively. Doubling the values in Equations (10) and (11) is necessary to gain the diameter of  $R_{s_i}$  and  $U_e$  of each sensor.

3.2.2. Categorization of Coverage Probability Based on PSM. In WSN, the best signal of the sensor node is based on the sensing range. There are two popular types of sensing models, which are used to enhance the sensing range in WSN. The first model is called Binary Sensing Model (BSM), and the second model is called Probability Sensing Model (PSM) [60]. The BSM supposed that the sensor node can detect each point if the point is within its sensing range. On the other hand, PSM, which is considered more realistic and more precise than BSM, takes in practice several dependent factors instead of the sensing radius that is used in BSM. These factors have no associated uncertainty in BSM such as noises and interferences among sensors that can affect the coverage value negatively and minimize the signal intensity [61, 62]. The coverage probability of PSM is shown in Figure 4 and calculated in Equation (12) [60].

$$\operatorname{Prob}_{\operatorname{cov}}(s_{i}, \boldsymbol{t}) = \begin{cases} 1 & \text{if } d(s_{i}, \boldsymbol{t}) \leq R_{s_{i}} - U_{e}, i = 1 \text{ to } \boldsymbol{n}, \\ e^{-\left(\frac{\alpha_{1} \lambda_{1}}{\lambda_{2}^{\beta_{2}}} + \alpha_{2}\right)} & \text{if } R_{s_{i}} - U_{e} < d(s_{i}, \boldsymbol{t}) < R_{s_{i}} + U_{e}, \\ 0 & \text{if } d(s_{i}, \boldsymbol{t}) \geq R_{s_{i}} + U_{e}, \end{cases}$$

$$(12)$$

where  $R_{s_i}$  and  $U_e$  are calculated according to Equations (1) and (2), whereas  $d(s_i, t)$  is the calculated distance between the position of the sensor node  $s_i$  and the position of target point t in the AoI. This distance is considered the real Euclidean distance between  $s_i$  and t in AoI as shown in Equation (13) [2]:  $R_s$ .

$$d(s_i, t) = Q_i \left( \sqrt{(x_{si} - x_t)^2 + (y_{si} - y_t)^2} \right), \quad i = 1 \text{ to } n, \quad (13)$$

where  $Q_i$  is the different sensing ranges that used for

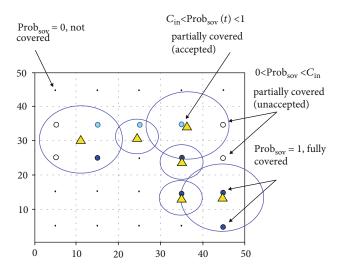


FIGURE 5: Categorization of target points based on the coverage probability of PSM.

covering the AoI, whereas x and y are the coordinates for each  $s_i$  and t. The parameters  $\alpha_1$ ,  $\alpha_2$ ,  $\beta_1$ , and  $\beta_2$  are representing the physical characteristics of the sensor unit and are supposed to be:  $\alpha_1 = 1$ ;  $\alpha_2 = 0$ ;  $\beta_1 = 1$ ; and  $\beta_2 = 0.5$  for each type, whereas  $\lambda_1$  and  $\lambda_2$  are considered as input parameters and calculated by the following equations [57, 62, 63].

$$\lambda_1 = U_e - R_{s_i} + d(s_i; t),$$
 (14)

$$\lambda_2 = U_e + R_{s.} - d(s_i; t).$$
 (15)

In PSM, the overlapped region occurs when the target point t exists in the overlapping region for the set of sensors  $S_{ov}$ . Thus, the probability of overlapping coverage in PSM would be calculated by the following equation [62].

$$\operatorname{Probs}_{\operatorname{ov}}(t) = 1 - \prod_{s_i \in S_{\operatorname{ov}}} \left( e^{-\frac{\left(\alpha_1 \times \lambda_1^{\beta_1}\right)}{\lambda_2^{\beta_2}}} + \alpha_2 \right), \quad i = 1 \text{ to } n,$$
(16)

where  $s_i$  is the sensor type. The  $Probs_{ov}(t)$  value was based on a coverage threshold value ( $C_{th}$ ) and was divided into four categories:

- (1) If  $Probs_{ov}(t) = 1$ , the target point is completely covered as illustrated in Figure 5 in a blue dark circle (acceptable)
- (2) If  $C_{\rm th} < {\rm Probs}_{\rm ov}(t) < 1$ , i.e., the target point is (partially covered—considered covered), as illustrated in Figure 5 in a sky blue circle (acceptable)
- (3) If  $0 < \text{Probs}_{\text{ov}}(t) < C_{\text{th}}$ , i.e., the target point is (partially covered—considered uncovered), as illustrated in Figure 5 in a blank circle (rejected)

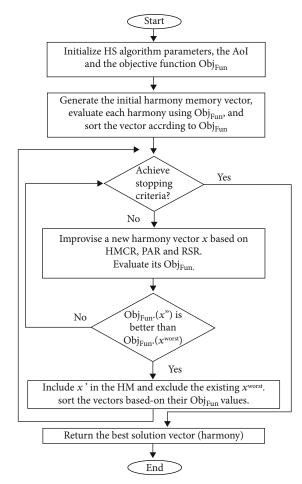


FIGURE 6: Steps of harmony search algorithm.

- (4) If  $Probs_{ov}(t) = 0$ , the target point is completely uncovered, as illustrated in Figure 5 in a filled circle (rejected)
- 3.3. Harmony Search Optimization. In this section, we introduce an engineering approach applied in the design and development of an algorithm, inspired by the improvisation process of the musical instruments to find fantastic harmony, called harmony search algorithm. It has received a great deal of attention regarding its potential as an optimization technique for solving discrete and continuous optimization problems. In HS, harmony parameters are typically used to create new harmony in each improvisation. The central role of these parameters is to direct the search toward the most desirable areas of the search space. These parameters are
  - (1) Harmony memory size (HMS) representing the total number of harmonies in the HM
  - (2) Harmony memory consideration rate (HMCR) which represents the probability of picking up values from HM to the variables in the solution vector
  - (3) Random selection rate (RSR) representing the probability of randomly chosen feasible values from the

range of all possible values to the variables in the solution vector, formally

- (4) Pitch adjusting rate (PAR) representing the probability of further adjusting the pitch with neighboring pitches
- (5) The number of improvisations (NI) representing the number of iterations to be used during the solution process, or stopping criterion

HS algorithm starts with an initial HM of \$n\$ harmonies generated randomly. Each harmony in the harmony memory represents a potential solution to the problem under consideration. These solution vectors are represented by the number of sensor node positions which are represented in real numbers. For HEWSN, the solution vectors are produced from AoI dimensions randomly and kept in HM. Each harmony in the harmony memory is evaluated using an objective function. The objective function used to measure the better quality of the solution vector is described in Subsection 3.3.1. The harmonies evolve through successive iterations, called improvisations. During each improvisation, a new harmony is created through harmony operators. After that, the harmony memory is updated if the new harmony is better than its worst one. The procedure continues until the termination condition is satisfied. When the termination condition is satisfied, the best harmony obtained is regarded as an optimal or approximate optimal solution to the problem. Figure 6 shows the optimization steps of HS, which is presented in detail in the next subsections.

3.3.1. Initialize the Algorithm and Problem Parameters. HS algorithm parameters that are required to solve the optimization problem (i.e., HMS, HMCR, PAR, BW, and NI) are specified in this step. These parameters are used to improve the solution vector. The probability of performing HMCR operation is chosen in such a way so that the inheritance of existing strings in HM occurs without disruption. Generally, HMCR rate lies between 0.7 and 0.95. Since PAR occurs occasionally, it is clear that the probability of performing PAR operation will be quite low. Usually, the PAR rate lies between 0.10 and 0.30. Values in these ranges help the algorithm to strike a balance between exploration and exploitation.

The objective function (Obj<sub>Fun</sub>) is the most important function for the optimization algorithms, where the best Obj-Fun is proved the effectiveness of the optimization algorithm. The  $Obj_{Fun}$  can be used to handle each generated solution vector which includes a group of sensor node positions. For the present problem, we have to maximize the coverage ratio of the network and minimize the number of added mobile nodes to the network, which is defined by the objective function. In other words, it is employed to scale the fittest of the positions and number of sensor node deployment. Each sensor node position is presented in real number and occurs at x  $_{\rm th}$  row and  $y_{\rm th}$  column. Therefore, to maximize the coverage and minimize the number of sensors deployment, the objective function is calculated based on network coverage ratio  $(C_{\text{ratio}})$ , HEWSN cost, and the minimum distance (MD). The objective function is depicted in the following equation.

$$Obj_{Fun} = \left(\frac{1}{SensCost}\right) \times C_{ratio} \times MD,$$
 (17)

where the SensCost is defined as the cost of the number of sensor deployment and is calculated based on the following equation.

$$SensCost = \frac{(HES_{no} - Min_{noS})}{Max_{noS} - Min_{noS}},$$
 (18)

where  $\text{HES}_{\text{no}}$  is the number of heterogeneous sensor deployment, and the aim is to be minimized, whereas Max  $_{\text{no}_{S}}$  and Min  $_{\text{no}_{S}}$  are calculated using Equations (10) and (11).

The coverage ratio ( $C_{\text{ratio}}$ ) is used to scale the QoS in the Obj<sub>Fun</sub> of the proposed algorithm, where the aim is to be maximized.  $C_{\text{ratio}}$  is computed by the following equation [57]:

$$C_{\text{ratio}} = \frac{N_{Eff}}{\left(\text{Cells}_{W_{\text{Dim}}} \times \text{Cells}_{H_{\text{Dim}}}\right)},\tag{19}$$

where  $N_{Eff}$  is the number of positions that are covered adequately and is calculated based on  $\operatorname{Probs}_{\operatorname{ov}}(t)$  value in Equation (16), whereas ( $\operatorname{Cells}_{W_{\operatorname{Dim}}} \times \operatorname{Cells}_{H_{\operatorname{Dim}}}$ ) is the dimensions of whole AoI that was calculated in Equations (3) and (4).

MD is the minimum distance between sensors, where the aim is to prohibit the unwanted convergence between sensors that may happen through the construction procedure of the proposed method, and it is computed in the following equation.

$$MD = \frac{MD(s_i, s_j)}{MAX (Diagonal)}$$
 (20)

where the numerator is used to compute the minimum distance between sensors and is calculated in the following equation.

MD (Si, Sj) = 
$$S_i^n \left( S_j^n \left( \sqrt{(xs_i - xs_j)^2 + (ys_i - ys_j)^2} \right), (21) \right)$$

where  $S_i^n$  and  $S_j^n$  are the permutations of sensing range types for the deployment sensors.  $xs_i$  and  $ys_i$  are x-axis and y-axis of each sensor, respectively. For example, if any study has two types of sensors with different sensing ranges, the probabilities of MD will be calculated exponentially such as  $2^n$ . So, the complexity will be increased with increasing types of sensors with different sensing ranges.

The diagonal means the length of diagonal AoI. So, the divisor of  $Obj_{Fun}$  in Equation (20) is used to compute the diagonal for each type and then selects the largest one to reach the minimum value of MD. The diagonal for each type is calculated in the following equation.

Diagonal = 
$$\sqrt{(W - R_{s_i} - U_e)^2 + (H - R_{s_i} - U_e)^2}$$
, (22)

where W and H are the width and height of the AoI, whereas  $R_{s_i}$  and  $U_e$  are calculated in Equations (1) and (2), respectively.

3.3.2. Initialize the Harmony Memory. Initialize the HM matrix ( $N \times HMS$ ), where N is the number of decision variables, and M is HMS. Then fill the HM randomly by generating the feasible solution vectors. For each decision variable ( $s_i$ ), lower<sub>si</sub>  $\le$  si  $\le$  upper<sub>si</sub>, where lower<sub>si</sub> and upper<sub>si</sub> represent the lower and upper boundaries of allowed values, respectively. Formally, HM and the corresponding fitness function values are shown as follows:

$$\text{HM} = \begin{bmatrix} x_1^1 & x_2^1 & \cdots & x_{N-1}^1 & x_N^1 \\ x_1^2 & x_2^2 & \cdots & x_{N-1}^2 & x_N^2 \\ \vdots & \cdots & \cdots & \cdots & \vdots \\ x_1^{\text{HMS}-1} & x_2^{\text{HMS}-1} & \cdots & x_{N-1}^{\text{HMS}-1} & x_N^{\text{HMS}-1} \\ x_1^{\text{HMS}} & x_2^{\text{HMS}} & \cdots & x_{N-1}^{\text{HMS}} & x_N^{\text{HMS}} \end{bmatrix} \stackrel{\Rightarrow}{\Rightarrow} f(X^1),$$

$$\Rightarrow f(X$$

where  $[x_1^i x_2^i \cdots x_{N-1}^i x_N^i]$  represents the feasible solution vector  $X^i$  in the harmony memory, and  $f(X^i)$  represents its corresponding objective function. The width (N) in Equation (23) of each solution vector can be modified and allowed each solution vector to encode a various number of sensors. The modifying in length grants the ability of HSA to select the optimal number of sensors as well as its optimal positions. Thus, to achieve this ability, the proposed work needs calculating range depending on the given network to avoid the extra computational demands and the false variable decisions on the number of nodes as mentioned in Equations (10) and (11). In addition, the length of each harmony memory vector represents as  $HMV_{length}$ , will vary between  $Min\_no_s$  and  $Max\_no_s$  parameters, and is computed by the following equation.

$$HMV_{length} = Min \_no_s + (Max_{nos} - Min_{nos}) \times rand () (24)$$

where Min\_no $_s$  and Max\_no $_s$  are calculated as Equations (10) and (11), respectively. The following example explains the role of HMV<sub>length</sub>on the enhancement of the network coverage and minimizing the cost of the network in heterogeneous case.

Example 1. Assume existence AoI with the size of  $(50 \times 50 \text{ m}^2)$  and many requirements such as finding the number of the optimal sensor with optimal positions. For example, two types of sensor nodes have various sensing range  $(R_{s_i})$  10 and 5 meters, respectively. Uncertainty values of  $U_e$  are assumed to be half of  $R_{s_i}$  for each one. Therefore, Min \_no\_s is computed in Equation (10) and equal to 3 and 11 sensors, respectively, while Max \_no\_s is calculated in Equation (11) and equal to 25 and 100 sensors, respectively. Thus, the HMV<sub>length</sub> is mod-

ifying between (3 and 100) sensors. Assume one of the harmony memory vectors that have 5 node positions and monitored by 5 sensor nodes:

#; #; 2.4; 5.8 #; #; 12.5; 16.8; #; #; 33.2; 3.4; 15.7; 44.8; #; #; #; 8; 7.2; :::

In the previous vector, the *x*-axis and *y*-axis of the first node are (2.4 and 5.8), the positions of the second node are (12.5 and 16.8), the positions of the third node are (33.2 and 3.4), the positions of the fourth node are (15.7 and 44.8), and finally, the positions of the fifth node are (8 and 7.2). The positions which signed with "#" are unused positions and are encoded to make the length of the HMV<sub>length</sub> to be as the Max \_no<sub>s</sub>. In the end, every harmony memory vector is generated with a various number of candidate sensor node positions. Hence, the proposed Obj<sub>Fun</sub> will measure and compute the quality of each harmony memory vector as the quality of the network coverage and cost as defined in step 1. The unused factor "#" that may exist in the harmony memory vector is deleted, and the rest of the components are employed to cover the AoI.

3.3.3. Improvise a New Harmony. A new Harmony vector  $X' = (x_1' x_2' \cdots x_N')$  is generated based on three parameters: memory consideration, pitch adjustment, and random selection which are modified to matching the WSN nature as follows.

For each component  $x_i'$  pick up the corresponding component of  $x_i^j$  randomly from any of the values in the specified HM range  $(x_i^1 - x_i^{\text{HMS}})$  with the probability of  $P_{\text{hmcr}}$ .

$$x_{i}' \leftarrow \begin{cases} x_{i}' \in \left\{ x' = \left(x_{i}^{1}, x_{i}^{2}, \dots : x_{i}^{\text{HMS}} & \text{with prob.HMCR} \right. \right\} \\ x_{i}' \in Xi & \text{with prob.} (1 - \text{HMCR}) \end{cases}$$
(25)

For example, the values of the x-axis  $(x_{si}^{-1}, x_{si}^{-2}, x_{si}^{-3}, \cdots, x_{si}^{-1}, y_{si}^{-1}, y_{si}^{-1}$ 

After the harmony memory considering factor is completed, change  $x_i'$  with the probability of  $P_{\rm par}$ . The pitch adjustment is applied only if the value is chosen from the HM. The pitch adjustment procedure is illustrated in the following equation.

Pitch adj. dec.for 
$$x_i' \leftarrow \left\{ \begin{array}{l} \text{Yes with prob.PAR,} \\ \text{No with prob.} (1 - \text{PAR}). \end{array} \right\},$$
 (26)

Parameter		Value
A C: ( ( ( ) T)	AoI 1	$50 \times 50 \text{ m}^2$
Area of interest (AoI)	AoI 2	$100 \times 100 \text{ m}^2$
Size of each cell		10 m
Maximum iterations number (MItr)		60000 iterations
Promotion and a manufacture	AoI 1	12 runs of each scenario
Experiments number	AoI 2	10 runs of each scenario
Coverage threshold ( $C_{\rm th}$ )		0.9
Parameters describing the sensing nodes.	$lpha_1$	1
	$lpha_2$	0
	$oldsymbol{eta}_1$	1
	$oldsymbol{eta}_2$	0.5
Uncertainty range $(U_e)$		5 and 2.5
IIi (IIMC)	AoI 1	30 vectors
Harmony memory size (HMS)	AoI 2	50 vectors
Harmony memory consideration rate (HMCR)		90%
Pitch adjustment rate (PAR)		0.3
Bandwidth distance (BW <sub>range</sub> )		0.2
Runs		Over 30 runs

If the pitch adjustment decision for  $x'_i$  is yes, then the small amount bw of changes takes place for pitch adjustments:

$$x_i' \leftarrow x_i' \pm BW_{\text{range}} * \text{rand} ()$$
 (27)

where the parameter BW<sub>range</sub> is the distance bandwidth which is used to modify the new node position value. The change is applied for the values of the x-axis and the y-axis of the corresponding  $x'_i$ .

3.3.4. Harmony Memory Update. Evaluate the new harmony  $x' = (x_1'x_2' \cdots x_N')$  by calculating its objective function  $Obj_{Fun}$  using Equation (23). If the value of its  $Obj_{Fun}$  is better than that of the worst harmony  $x^{worst}$  in the HM, x' is included in the HM, and the existing  $x^{worst}$  is excluded from the HM. Subsequently, the vectors are sorted based-on their  $Obj_{Fun}$  values.

3.3.5. Termination Criterion Check. In this step, repeat steps 3 at Subsections 3.3.3 and 4 at Subsection 3.3.4 until the termination criterion is met. The solution vector in HM that can achieve maximizing coverage and minimizing the number of sensors deployment is selected to be the best solution vector.

#### 4. Experimental Results and Comparative Study

4.1. Simulation Setup. The simulation environment is based on PSM and HEWSN random deployment using HSA. The simulations were applied over two different areas in three scenarios for each one. In the first area, the AoI is designed

to be  $50 \times 50 \,\mathrm{m}^2$  dimension area which is separated into 25 cells and all results based on 25 sensors as a maximum number of sensor deployment. In the second area, the AoI is designed to be  $100 \times 100 \,\mathrm{m}^2$  dimension area which is separated into 100 cells and all results based on 50 sensors as a maximum number of sensors deployment. Most of the simulation parameters in Table 1 are set according to [57]. The measure of cell in each scenario is set to be 10 m, as mentioned in Figure 3. The sensing range  $R_s$  has two types A and B, where type A is set to be 10 m and type B set to be 5 m. The uncertainty in sensor detection  $R_e$  is set to be half of the sensing range  $R_s$  (means 5 and 2.5, respectively). The coverage threshold  $C_{\rm th}$  is set to be 0.9, whereas the PSM's parameters are set to be  $\alpha_1 = 1$ ;  $\alpha_2 = 0$ ;  $\beta_1 = 1$ , and  $\beta_2 = 0.5$ .

The values of  $\lambda_1$  and  $\lambda_2$  are calculated based on Equations (14) and (15). In addition, the minimum and maximum numbers of sensors that achieved the network requirements are calculated according to Equations (10) and (11), respectively. Finally, the simulation worked on a computer that has windows 7, core i5-3470, 8 GB RAM, and CPU 3.20 GHz. More details about simulation environment parameters are illustrated in Table 1.

The HMCR and PAR are two fundamental parameters in HSA. They are used to set the probability of components stored in HM. If the value of HMCR is extremely high (near 1), almost all the harmonies are used in the HM. Therefore, typically, we used HMCR = 90% and the HMS = 30 solution vectors as the work in [11].

On the other hand, a low PAR with a little value of bandwidth can slow down the convergence of HSA. However, a very high PAR with a high-value bandwidth may also lead to wrong solutions [64]. Thus, the applications usually

Cell size vs. sensing range	HEWSN deployment 10(10,5)			
	S1	S2	S3	
Number of runs	12	12	12	
Maximum number of node sensors (MN)	25	25	25	
Best (maximum coverage ratio)	96%	100%	100%	
Number of corresponding sensors	16HES = (12HOS)	18  HES = (13.5 HOS)	17HES = (12.5HOS)	
Corresponding sensor ratio	48%	54%	50%	
Average of each scenario	88%	92%	94%	

TABLE 2: Results of HEWSN deployment based on HSA.

Table 3: The best minimum cost of HEWSN deployment based on HSA.

Cell size versus sensing range	HEWSN deployment 10(10,5)
Maximum number of node sensors	25
Number of corresponding sensors	17HES = $12.5$ HOS
Best (maximum coverage ratio)	100%
Corresponding sensor ratio	50%
Cost	50%

Table 4: The best result of HEWSN deployment over  $100 \times 100 \text{ m}^2$ .

Cell size versus sensing range	10(10,5)		
Scenarios of AoI 2	S1	S2	S3
Maximum number of node sensors (MN)	50	50	50
Number of runs	10	10	10
Number of corresponding sensors	42	45	49
Best (maximum coverage ratio)	79%	88%	90%
Corresponding sensor ratio	64%	67%	73%
Average of each scenario	69%	76%	82%
Cost	15%	21%	17%

use PAR = 0.1 to 0.5. PAR value = 0.3 which means that the neighboring value will be chosen with a 30% probability [11].

The proposed model is benchmarked against the baseline cases of sensor network deployment [11]. Several metrics are selected to evaluate the efficiency and effectiveness of the proposed model named coverage ratio, the minimum number of sensors deployment (network cost), and reducing the overlap among sensor nodes. The parameters that are mentioned in Tables 2–5 such as corresponding sensors ratio (Corr<sub>ratio</sub>) and cost are calculated in Equations (28) and (29).

The coverage ratio ( $C_{\rm ratio}$ ) was given in Equation (19), and the corresponding sensors ratio ( ${\rm Corr}_{\rm ratio}$ ) is calculated by Equation (28) and depicted in Equation (29).

$$Corr_{ratio} = (corresp. No. of sensors \div MN) \times 100,$$
 (28)

where the corresponding number of sensors means the number of deploying sensors, whereas MN means the maximum number of deploying sensors. The minimum number of deploying sensors (network cost) is calculated based on Equation (28).

$$Cost = C_{ratio} - Corr_{ratio}.$$
 (29)

4.2. Simulation Results. Three simulation scenarios have been created to show the performance of the proposed model in both AoI of size  $50 \times 50 \, \text{m}^2$  and AoI of size  $100 \times 100 \, \text{m}^2$ . For comparison purposes, the proposed model in HEWSN deployment has been simulated, and the simulation results of HSA in HOWSN deployment have been inserted. The performance of the proposed model has been evaluated in three metrics: maximizing coverage, minimizing network cost, and reducing the overlap of sensor nodes using MATLAB simulator. The three scenarios of the proposed model are explained in the following subsections.

4.2.1. Scenarios of the Proposed Model over AoI 1. The proposed model conducted three scenarios to confirm the efficiency and effectiveness of the proposed deployment model for solving the network coverage and cost problems in WSN. Each scenario executes 12 runs, as presented in Table 2. One best result of each scenario was chosen depending on the best minimum number of HEWSN random deployment to offer an efficient solution for coverage problem as follows.

(1) Maximizing Coverage of HEWSN Based on HSA. The first part of the main problem which is investigated is to maximize the coverage. Each scenario used 25 sensors as the maximum number of deployed sensors. In the best result of the first scenario, the corresponding number of deploying sensors is 16 out of 25 sensors (8 sensors with sensing range 5 m and 8 sensors with sensing range 10 m) as illustrated in Figure 7. In the best result of the second scenario, the proposed model used less number of sensors, where the corresponding number of deploying sensors is 18 out of 25 sensors (9 sensors with sensing range 5 m and 9 sensors with sensing range 10 m) as illustrated in Figure 8. Finally, in the best result of the third scenario, the best corresponding number of deploying sensors is 17 out of 25 sensors (9 sensors with sensing range 5 m and 8 sensors with sensing range 10 m) as illustrated in Figure 9.

It is clear from the results shown in Figures 7–9, the coverage ratio of HSA increases with the decreased number of sensors. The first best result that is obtained in Figure 7

Call size versus sensing range	HEWSN deployment 10(10,5)				
Cell size versus sensing range	S1	S2	S3	S4	S5
Maximum number of node sensors (MN)	25	25	25	30	35
Number of runs	12	12	12	12	12
Number of corresponding sensors	<b>20HES</b> = <b>15 HOS</b>	22HES = 16.5HOS	23 HES = 17 HOS	$\mathbf{27HES} = \mathbf{20.5HOS}$	34HES = 23.5 HOS
Best (maximum coverage ratio)	56%	60%	60%	68%	84%
Corresponding sensor ratio	60%	66%	68%	58%	61%
Average of each scenario	44%	50%	55%	60%	67%

Table 5: Results of HEWSN deployment based on GA.

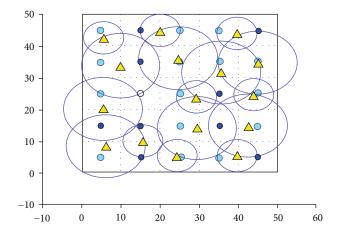


FIGURE 7: Best result of first scenario in HEWSN deployment with 10 m and 5 m using 16HES = 12HOS sensors based on HSA.

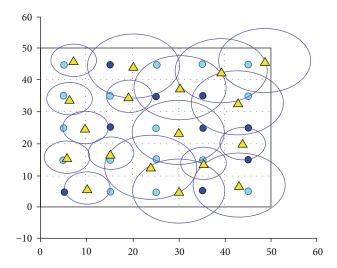


FIGURE 8: Best result of the second scenario in HEWSN deployment with 10 m and 5 m using 18HES = 13.5HOS sensors based on HSA.

shows that the coverage of the proposed model was near the full coverage, where the coverage ratio reached at 96% when the corresponding number of deploying sensors is 16 sensors and the corresponding sensor ratio is 48%. In the second result, the coverage ratio reached 100% and 54% of the corresponding sensor ratio when the corresponding number of

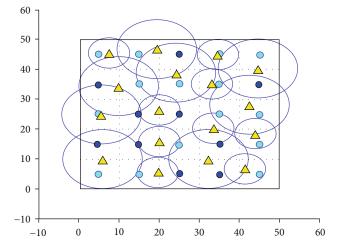


FIGURE 9: Best result of the third scenario in HEWSN deployment with 10 m and 5 m using 17HES = 12.5HOS sensors based on HSA.

deploying sensors is 18 sensors, as shown in Figure 8. The third result in Figure 9 shows the best performance of the proposed model that has an ability to cover all of the targets and find the optimal positions of the deploying sensor nodes with a minimum number of sensors. Table 2 summarized the best results of the three scenarios based on the proposed model. The average coverage ratio for 12 runs in each scenario was 88%, 92%, and 94%.

(2) Minimizing Cost of HEWSN Based on HSA. The second part of the main problem, which is also investigated to minimize the network cost. The number of cells in the AoI 1 is equal to the maximum number of deployed sensors. Table 3 shows a summary of HEWSN with the best minimum cost based HSA as follows.

As shown in Table 3, the cost of the best result of HEWSN deployment was reduced by 50% when the number of corresponding sensors is equal to 12.5 HOS out of 25 sensors.

4.2.2. Scenarios of the Proposed Model over AoI 2. In this scenario, the proposed model was investigated to offer an efficient solution for coverage and cost problems in a broad area. The cost consideration for the number of sensors deployment in a small area can be determined, but to cover

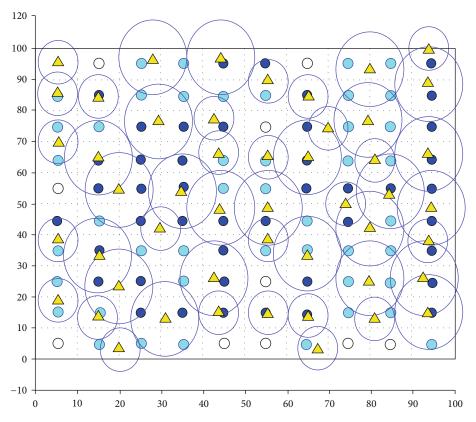


Figure 10: Best result of AoI  $100 \times 100 \,\mathrm{m}^2$  based on HSA.

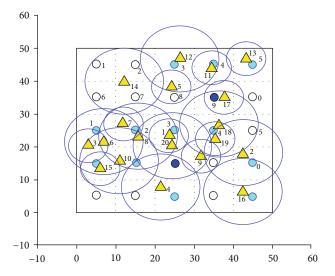
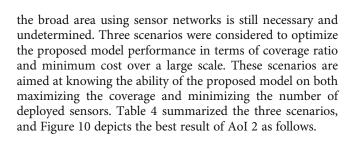


FIGURE 11: Best result of first scenario in HEWSN deployment with 10 m and 5 m using 20HES = 15HOS sensors based on GA.



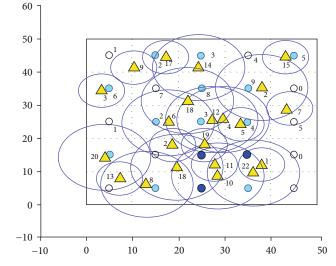


FIGURE 12: Best result of the second scenario in HEWSN deployment with 10 m and 5 m using 22HES = 16.5HOS sensors based on GA.

As shown in Table 4, the coverage ratio reached at 90% when the number of deploying sensors equal to 49 out of 50 sensors. The average of the best scenario was 82%, and the cost was reduced by 17%.

4.3. Comparative Study. This section presents two comparisons, the first comparison between the proposed model and GA in HEWSN and the second comparison between HSA

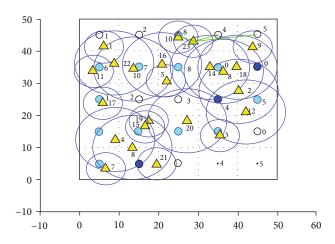


FIGURE 13: Best result of the third scenario in HEWSN deployment with 10 m and 5 m using 23HES = 17HOS sensors based on GA.

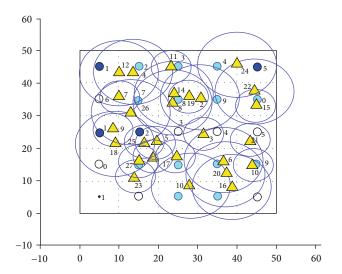


Figure 14: Best result of  $4^{th}$  scenario using 27 sensors deployment based on GA.

and GA in HOWSN. Both comparisons have been evaluated into two metrics, maximizing coverage and minimizing cost as follows.

4.3.1. Scenarios of Genetic Algorithm (GA). In Genetic Algorithm, the group of solutions is known as chromosomes. These chromosomes represent a group of sensor node positions and are stored in population, which is equivalent to Harmony Memory in Harmony Search. In each generation of GA, a set of population size chromosomes is known as offsprings. In our scenarios, a population size is equal to 50, GA terminates after 1,000 generations, and a single point crossover operator is used with a probability of Pc = (0.80).

For the mutation operator, if a generated random number is with a probability of Pm = (0.025), each gene in the offspring can be modified using Equation (27). The values of both Pm and Pc are taken according to the comparison application in [11].

In the previous section, the simulation results are executed to investigate the performance of the proposed

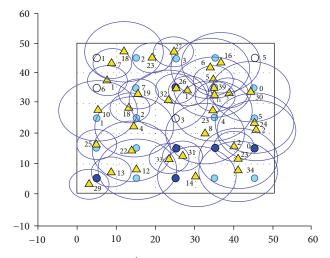


FIGURE 15: Best result of 5<sup>th</sup> scenario using 34 sensors deployment based on GA.

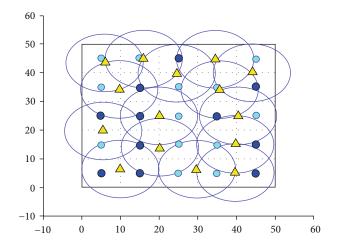


FIGURE 16: Best result of HOWSN deployment with 10 m using 15 sensors based on HSA.

model. In this section, three scenarios are introduced in this simulation using 12 runs. One best result of each scenario is chosen depending on the best minimum number of HEWSN random deployment as illustrated in Figures 11–13. In the best result of the first scenario, the corresponding number of deploying sensors is 20 out of 25 sensors (10 sensors with sensing range 10 m and ten sensors with sensing range 5 m) as illustrated in Figure 11. In the best result of the second scenario, the corresponding number of deploying sensors is 22 out of 25 sensors (11 sensors with sensing range 5 m and 11 sensors with sensing range 10 m) as illustrated in Figure 12. In the best result of the third scenario, the corresponding number of deploying sensors is 23 out of 25 sensors (12 sensors with sensing range 5 m and 11 sensors with sensing range 10 m) as illustrated in Figure 13.

As shown in Figure 11, the coverage ratio reached at 56% when the corresponding number of deploying sensors equal to 20 sensors, and the corresponding sensor ratio is 60%. In the second and the third-best results, the coverage ratio reached

Parameters	HEWSN (HSA)	HEWSN (GA)	HOWSN (HSA)	
Number of runs	Over 30	Over 30	Over 30	
Cell size versus sensing range	10(10,5)	10(10,5)	10(10)	
Maximum number of sensors	25	35	25	
Corresponding sensors	12.5	34HES = (23.5HOS)	15	
Best (maximum coverage ratio)	100%	84%	100%	
Corresponding sensor ratio	50%	61%	60%	
Cost minimization by	50%	23%	40%	
Average of (best scenario)	94%	67%	93%	

TABLE 6: Best result comparison between HEWSN and HOWSN deployment based on HSA and GA.

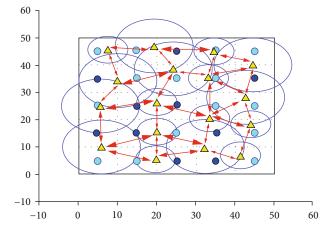


FIGURE 17: The impact of overlapping on the best result of the proposed model.

at 60% when the corresponding number of deploying sensors equal to 22 and 23 and the corresponding sensor ratio equal to 66% and 68% as shown in Figures 12 and 13, respectively.

Moreover, and to be more precise, GA dose did not reach maximum coverage ratio with a minimum number of sensors (15 of HOWSN or 17 of HEWSN), but it can be reached at 68% as the best result of the 4<sup>th</sup> scenario when the corresponding number of deploying sensors equal to 27 and the maximum number of sensors deployment equal to 30 as shown in Figure 14. Also, it can be reached at 84% as the best result of the 5<sup>th</sup> scenario when the corresponding number of deploying sensors equal to 34 sensors and the maximum number of sensor deployment equal to 35 as shown in Figure 15. Table 5 is summarized the best results of the five scenarios based on GA.

As shown in Table 5, the best results of the 4<sup>th</sup> and 5<sup>th</sup> scenarios increased with the increasing number of deployed sensors. The coverage ratio of the 4<sup>th</sup> scenario reached 68% when the number of deploying sensors equal to 27. In addition, it reached 84%, i.e., with increasing 16%, when the number of deploying sensors identical to 34 sensors as in the 5<sup>th</sup> scenario. The average coverage ratio of HEWSN random deployment in each scenario based on GA was 44%, 50%, 55%, 60%, and 67%, respectively.

4.3.2. The Comparison of the Proposed Model with HSA in HOWSN. For comparison purpose, Figure 16 in [11] illus-

trated the best simulation result of HOWSN deployment based on HSA.

As shown in Figure 16, the coverage ratio reached at 100% when the corresponding number of deploying sensors is 15 out of 25 sensors with a 60% corresponding sensor ratio. The cost of HOWSN deployment was reduced by 40%, whereas the average coverage ratio was around 93% for all results.

Table 6 illustrates the comparison between the proposed model and both GA and HSA in HEWSN and HOWSN random deployment, respectively.

As shown in Table 6, the coverage ratio of HEWSN based GA increases with an increased number of corresponding deploying sensors. The coverage ratio reached 84% when the number of corresponding sensors was 34 sensors. In addition, the cost was reduced by 23%. In other words, GA can be reached near full coverage when the number of deploying sensors was more than the number of cells.

In summary, the proposed model introduced the superiority against GA in HEWSN and increased by about 16% and 27% in terms of coverage ratio and cost, respectively. In addition, the cost of HOWSN based on HSA was reduced by 40%, whereas the cost of HEWSN deployment was reduced by 50%. Moreover, the coverage ratio of the proposed model was 94%, whereas it was 93% in HOWSN based on HSA.

4.4. The Impact of Minimum Overlapping on the Proposed Deployment Model. The third metric is to minimize the overlapping coverage area in WSN with nodes having a different radius. This section illustrates the impact of the decreasing overlap between sensors that are introduced in the  $\mathrm{Obj}_{\mathrm{Fun}}$  of the proposed model. In fact, the MD operator is defined to prevent the deployed sensors from being close to each other and then avoid the network from overlapping problem, i.e., avoid an extra cost of the unnecessary deployed sensors. In other words, the coverage ratio is maximized by minimizing the overlap problem. It is clear that the overlap among sensors in Figure 9 was low. Each sensor is about the same distance from the other sensor.

In addition, Figure 9 can be able to obtain the best network coverage due to all target points were covered with a minimum network cost. On the other hand, Figure 15 has the least displacement among sensors, where the number of sensors that are used to cover the network is higher than that in Figure 9. It used 34 sensors close to each other and then the coverage was minimized by around 16% (the rest to reach

maximum coverage 100%). This means that (Figure 15) the number of demanded sensors to get maximum coverage is to be around 40 sensors. This extra 23 (the extra numbers to 17 sensors of best Figure 9) sensors can increase the network cost by around 42% compared to the best result in Figure 9. Figure 17 shows the impact of overlapping on the best result of the proposed model.

#### 5. Conclusion

In this paper, we addressed the problem of maximizing the coverage and minimizing the number of deployment of sensors in HEWSN using HSA and PSM. One of the main contributions of our work is to update and reformulate the equations that are used in PSM for homogeneous wireless sensor network and to evaluate the proposed deployment model by comparison with the existing method based on HSA. The proposed work introduced heterogeneous sensor network deployment based on the probabilistic sensing model (PSM) and harmony search algorithm (HSA). PSM is used to enhance the probability of coverage without interference. Here, HSA is used for optimizing the maximum coverage with the minimum number of sensors in HEWSN. The simulation results and quantitative analysis proved that the proposed model can provide solutions up to 100% of the coverage ratio over a small area. Also, it demonstrated the efficiency and superiority of the proposed algorithm in HEWSN random deployment with the minimum number of sensor nodes, where it reduced the network deployment cost by a factor of 50% with a minimum overlapping.

On the other hand, the proposed work has evaluated the performance of the proposed algorithm with HSA in HOWSN random deployment. The results showed that the proposed model reduced the deployment cost by a factor of 10% by comparing with HSA in HOWSN deployment. Our contribution here is twofold. First, the minimum cost of heterogeneous sensors for PSM as the maximizing coverage in heterogeneous wireless sensor network (HEWSN) model has been reformulated, and second, using of HSA and PSM for providing optimum deployment in HEWSN.

#### **Data Availability**

The data (measured data and codes) used to support the findings of this study are available from the corresponding author upon request and with the institute's permission.

#### **Conflicts of Interest**

The author declares that they have no competing interests.

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