Research Article

Uncertainty and Sensitivity of Neutron Kinetic Parameters in the Dynamic Response of a PWR Rod Ejection Accident Coupled Simulation

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In nuclear safety analysis, it is very important to be able to simulate the different transients that can occur in a nuclear power plant with a very high accuracy. Although the best estimate codes can simulate the transients and provide realistic system responses, the use of nonexact models, together with assumptions and estimations, is a source of uncertainties which must be properly evaluated. This paper describes a Rod Ejection Accident (REA) simulated using the coupled code RELAP5/PARCSv2.7 with a perturbation on the cross-sectional sets in order to determine the uncertainties in the macroscopic neutronic information. The procedure to perform the uncertainty and sensitivity (U&S) analysis is a sampling-based method which is easy to implement and allows different procedures for the sensitivity analyses despite its high computational time. DAKOTA-Jaguar software package is the selected toolkit for the U&S analysis presented in this paper. The size of the sampling is determined by applying the Wilks' formula for double tolerance limits with a 95% of uncertainty and with 95% of statistical confidence for the output variables. Each sample has a corresponding set of perturbations that will modify the cross-sectional sets used by PARCS. Finally, the intervals of tolerance of the output variables will be obtained by the use of nonparametric statistical methods.

1. Introduction

Being able to simulate accurately the different transients that can occur in a nuclear power plant is one of the main aims in nuclear safety analysis. Transient simulations involve both neutronic and thermalhydraulic calculations which are solved by different computer codes using best estimate models. Even though this approach provides more realistic responses than conservative codes, because of the reduction of the conservatism, the uncertainty in the code predictions of relevant safety system variable resulting from assumptions and code model estimates must be carefully evaluated. Uncertainties may stem from various sources, for example, lack of knowledge, approximate character of physical models, uncertainty in model data, and so forth, and will be statistically propagated to code output parameters which have a probability density function and a range limit.

In order to obtain the uncertainties in the macroscopic neutronic information using a best estimate neutronicsthermalhydraulic coupled code, a Rod Ejection Accident (REA) has been simulatedm and the results are presented in this paper. The REA accident belongs to the reactivityinduced accidents (RIA) category and is part of the licensing basis accident analyses required for pressurized water reactors (PWR). The REA consists of a rod ejection due to the failure of its operating mechanism with the power evolution driven by a continuous reactivity insertion. The main factor limiting the consequences of the accident is the Doppler reactivity effect. The physical description of the reactor response is based on the coupled neutronicthermalhydraulic code RELAP5/PARCSv2.7. Since a coupled code is used for the best estimate analysis, uncertainties from both aspects should be included and jointly propagated. CASMO4-SIMULATE3 provides the cross-section sets which are processed using the SIMTAB methodology developed at the Polytechnic University of Valencia (UPV) together with Iberdrola [1].

With the objective of providing a realistic environment for the development of the dynamic behaviour, monitoring and adjustment procedures, dynamic models for monitoring and control the output system have been developed.

2. Statistical Methodology

2.1. Introduction. It is possible to quantify the uncertainty by means of statistical measures. For instance, even when the exact values for a given code input are unknown, a range of possible values that it can take may be available. It is then possible to quantify uncertainty by considering the range, and a probability density function (PDF) that assigns a probability to the values inside the range. Sometimes, however, a third factor has to be considered [2], namely, the model uncertainty, that is, the difference between the real system and the result predicted by a set of approximations depending on the used model.

In this work, both the tolerance limits and the PDF distributions were an assumption. The real values of the tolerance limits for each kinetic parameter and its PDF distribution type will be known only after a validated uncertainty propagation methodology is applied to the whole process. This process, consisting in neutron kinetic parameters generation for coupled 3D neutronic-thermalhydraulic, could be divided into three steps: (1) cell physics (derivation of the multigroup microscopic cross-section libraries and associated uncertainties), (2) lattice physics (derivation of the few-group macroscopic cross-section libraries and associated uncertainties), and (3) core physics (core steady-state and transient behavior with the associated uncertainties). Hence, this work is a general approach to the third step (core physics) on the assumption that the uncertainties corresponding to the first two steps are previously obtained.

Moreover, it is known that the fractions of delayed neutrons precursors (and their decay constants) play an important role in output variable variance. This influence depends on how far from prompt critical the insertion of reactivity is. Thus for small insertions of reactivity, delayed neutrons play an important role in the time evolution of the neutron flux, and so the uncertainty in β_i and λ_i will have a greater effect in the kinetic output variables. As the weight of the delayed neutrons decreases with the proximity to prompt criticality, the influence of β_i and λ_i also diminish as does the effect of their uncertainty.

In any case, the reason why the uncertainties in β_i and λ_i have not been included in this current study is the lack of available information. It is not expected, however, that maintaining these parameters unchanged will influence the

conclusions about the uncertainty and sensitivity results taking into consideration the uncertainties in the most important neutronic data considered in this work. The effects of the uncertainties on the kinetic parameters related to the precursors of delayed neutrons, however, will be taken into account in future studies.

The computer code plays the role as the used model and its associated uncertainty is calculated using the presented methodology. Figure 1 provides an easy explanation of the followed procedure (step 3).

The computer code is a deterministic function that transforms stochastic uncertain in its inputs and models, X_1 to X_n , into stochastic uncertainty associated to its outputs Y.

The coupled code is represented by the function f, which calculated the output variables Y, as a function of input variables, X_i , whose uncertainties can be determined. With sensitivity analysis, the importance of each X_i regarding its influence on the uncertainty of Y can be calculated and hence a numerical value to that influence can be assigned.

To get a proper understanding on what is actually happening in the model, it is also important to perform a sensitivity analysis. This type of analysis reflects the variance of one response random variable when an input related random variable is perturbed. In this work, the sensitivity analysis performed is based on statistical measures of correlation between the input variables selected as sources of uncertainty and those output variables of interest. Two kinds of correlations can be used, those based on regression analysis, for example, Pearson Product Moment, and those based on nonparametric Rank correlation, for example, Spearman regression coefficients. Pearson correlation is most suitable for linear dependencies, whereas Spearman correlation can better quantify nonlinear and linear dependencies. For this work, Spearman correlation has been selected to carry out the sensitivity analysis. Additionally, full and partial correlations have been computed and analysed. Full correlations include the effects of all the input variables simultaneously, and partial correlations can eliminate the effects of the other variables for a given one. A threshold value of ± 0.2 is usually accepted as a threshold value below which an input variable is considered to have no significant influence on an output variable. In the paper, we have selected a value of ± 0.16 for this purpose.

It is important to point out that statistical sensitivity measures only quantify statistical relationships and do not offer quantitative values about the magnitude of the relationship which could be used to further compute linear uncertainties in the output variables of interest. For this, analytical or numerically obtained first-order derivatives must be computed, ∂ Output/ ∂ Input, which is not always possible, especially for systems with nonlinear behaviour, for which second order and cross derivatives should be also included.

2.2. Methodology Description. This paper discusses a work based on previous studies [3]. The procedure followed to perform the uncertainty and sensitivity analysis is a sampling-based method. This method has been chosen because it is easy to implement, allows different procedures



FIGURE 1: Model with input and output variables, extracted from [2].

for the sensitivity analyses [4], and is suitable for all computer codes. One of its main advantages is that the user does not need to know beforehand the importance of each input variable since the order of importance is provided by the sensitivity analysis afterwards. However, the main drawback of the sampling-based methods is the high computational cost. Another important feature of the methodology is that the accuracy of the obtained results is not dependent on the number of input parameters but among other factors, as the sample size or even the sampling procedure randomness. The latter condition ensures the randomness in the output variables.

The first step in the methodology is the characterization of the input variables uncertainty. As a starting point, the user must decide which input variables could be more relevant or sensitive for the output variables. As stated earlier, two factors are used in order to define the uncertainties related to the input variables: the intervals of possible values and the PDF associated. The uncertainty analysis with nonparametric methods can lead to range limits for *Y* in the form (*lower limit, upper limit*). These limits contain the real value of *Y* with a certain probability, *p*, and a prescribed level of confidence, *y*. The lower and upper selected bounds for all input variables are (-0.003, +0.003).

Regarding the selection of the distribution, if there is no information or knowledge in order to provide a PDF for a certain X_i , the uniform distribution is recommended since it assigns equal probability to each value within the sample space. However, depending on the phenomena modelled, the selection of the normal or even the log-normal distribution could be a better choice. In this paper, the chosen PDF distributions are uniform and normal which presents three different standard deviations, 0.1%, 0.5%, and 1%, respectively, both with mean value equals to 0. Once the distribution type is chosen, the sample has to be generated.

Computer codes, in general, do not accept intervals as X_i , but rather a unique numerical value for each X_i . Thus the methodology must provide a value for each X_i within each interval. There are several statistical techniques which could provide the desired values but two methods were selected in this work: Random and Latin Hypercube Lattice Sample (LHS), which is described in Section 2.4.

The second step involves performing the simulations a certain N number of times. This action is equivalent to obtain Y as a function of different sampled X (each time with a different sampled X). An appropriate sample size value, N, is another important part of the methodology. This value depends on the desired uncertainty accuracy and is related with Wilks' formula which gives the minimum number of simulations and, hence, the number of input samples.

The Wilks' approach, also known as GRS's (Gesellschaft für Anlagen- und Reaktorsicherheit) method in nuclear safety field, is based on a pure statistical method [5]. The sample size, obtained by applying the Wilks' formula for double tolerance limits with a 95% of uncertainty and with 95% of statistical confidence for the output variables, is equal to 93 [6]. However, it has been recently published that the recommended minimum number of required code runs for the condition of 95/95 for 1st order two-sided approach are 146 [7], which is the code runs performed in this present work.

Each of the N simulations uses a different sampled X and leads to one different Y. In other words, N sets of X lead to N different output variables, Y. Furthermore, Y will be randomly provided due to the fact that X was randomly chosen. The PDFs of Y are sufficient to calculate the uncertainty in Y. However, the PDFs are not always easy to evaluate, thus, the only remaining alternative is to obtain as much information as possible about the PDFs properties together with the main parameters. One of the most used parameter is the quantile which comes from empirical PDFs and estimators.

The uncertainty of Y, for a certain uncertainty in X, can be easily calculated if Y is randomly sampled with a normal PDF. Provided those hypotheses, the tolerance intervals can be calculated with only two parameters: sample mean, m_y , and sample standard deviation, s_y . As stated earlier, the hypothesis of normal PDF for Y is not always easy to guarantee; however, there are some statistical tests that can be used to quantify how well the hypothesis of normality fits the sampled data. An important statistic test is the Rank correlation test for detecting linear relationship as well as nonlinear behaviour between X and Y. Examples of linear measures are the simple correlation coefficient (SCC), or Pearson's moment product, and the partial correlation coefficient (PCC). The most important advantage of the PCC is that it eliminates the linear influence of the remaining $X_{i,i\neq i}$ on Y, leaving only the X_i whose sensitivity is being calculated. Both Rank correlations, simple and partial, will be described in Section 2.3.

2.3. Simple or Partial Rank Correlation. In order to deal with models which are not clearly linear, simple (SRCC) or partial rank correlation (PRC) coefficients can be used. To calculate these two correlations, the sample values of X_i and Y, whose relationship has to be determined, are separately "ranked"; that is, two separate and ordered lists (in decreasing or increasing order) are created, followed by the assignment of a rank or an integer number to each value.

If the two "unranked" original series of values are related monotonously, then the ordered series are linearly related. This is true even if the relationship between the unordered series is not linear. Thus the absolute values of SRCC and PRCC will quantify the degree of relationship between the given X_i and Y_i of interest. The closer the values of these coefficients are to one, the more influence that X_i will have on Y. In sensitivity analysis, the most used test is the Spearman's coefficient. The critical values for the Spearman rank correlation coefficient are calculated by equation $r_s = \pm z/\sqrt{n-1}$, where n is the number of runs and z represents the point on the standard normal PDF. This point represents the probability, p, of observing a value greater than z, which is known as the upper critical value (quantile). For a confidence interval of 95%, z = 1.96.

2.4. Latin Hypercube Lattice Sample. For more than twenty years, the Latin Hypercube Lattice Sampling program has been successfully used to generate multivariate samples of statistical distributions. Its ability to use either Latin hypercube sampling or pure Monte Carlo sampling with both random and restricted pairing methods has made it an important part of uncertainty analyses in areas ranging from Probabilistic Risk Assessment (PRA) to complex simulation modelling.

Latin Hypercube Lattice Sampling (LHS) is a stratified random procedure that provides an efficient way of sampling variables from their distributions [4, 8, 9]. LHS is very popular for use with computationally demanding models because its efficient stratification properties allow for the extraction of a large amount of uncertainty and sensitivity information with a relatively small sample size. In fact, the main advantage of LHS respect Simple Random is that LHS gets a better dispersion sample points over the input domain space [10].

The LHS process consists of three steps: (1) the range of each input variable, X_i , is divided into n intervals with equal probability according to the associated PDF, (2) a random point is generated in each interval and for each input variable, and (3) one sample is generated with a random combination, without replacement, of the points randomly generated in step 2 (one point from each X_i). Step 3 is repeated for the N required samples. Since one point is randomly generated in each interval, the domain input space is efficiently covered.

3. DAKOTA Methodology

It is well known that some design parameters have a high influence on the response whereas the influence of other parameters can be neglected. In order to optimize the design process, sensitivity analysis techniques and parameter study methods are performed. Both techniques and methods are used for identifying which parameters could be needed and which could be taken as constant parameters. In addition, in a postoptimization role, sensitivity information is useful in determining whether or not the response functions are robust with respect to small changes in the optimum design point [11].

TABLE 1: Input file information summary.

Sample size	146
Input model variables	7
Lower bound	-0.003
Upper bound	+0.003
Sampling method	Random/LHS
Variables distribution	Uniform/normal

DAKOTA software, which stands for Design Analysis Kit for Optimization and Terascale Applications, is the selected toolkit for the present sensitivity analysis study. DAKOTA provides a flexible interface between analysis codes and iterative systems analysis methods [11]. Besides, DAKOTA is a very powerful tool that allows performing uncertainty quantification with sampling and sensitivity/variance analysis as well as a variety of more applications. The features implemented in DAKOTA lead to improved designs and system performance in earlier stages which may reduce development time and cost.

JAGUAR, which stands for JAva GUi for Applied Research, is a graphical wizard program which parses a DAKOTA input specification and serves as a graphical user interface (GUI) providing both graphical and text representations of the problem setup for DAKOTA studies afterwards [12]. Basically, JAGUAR is a friendly user interface that helps the user to introduce the data and calls DAKOTA for calculations.

For this specific uncertainty and sensitivity analysis, the studied input variables are the following seven neutronic parameters: diffusion coefficient which determines the leakage for thermal and fast group (*Diff1* and *Diff2*), scattering cross-section (*SigR*) which determines the moderation, absorption cross-section for both groups (*Siga1* and *Siga2*), and neutrons per fission multiplied by fission cross section which determines the rate of fission power release for both groups as well (*NuSigF1* and *NuSigF2*). The sample size and the selected sample methods and distributions were discussed previously. The described input file information is summarized in Table 1.

After settingup the input model file, the perturbation matrix file is generated. Both processes are part of the socalled *prerun* process in Jaguar. The size of the generated matrix is equal to the sample size multiply by the number of input model variables (i.e., 146×7) and each matrix element represents a perturbation parameter. The matrix file is used for modifying the cross-section sets by multiplying the 7 input model variables by the obtained perturbations. Each sample has a corresponding set of perturbations so it means that the number of simulations must be equal to the sample size. Even though, the REA analysis is performed by the coupled system RELAP5-PARCS, the cross-sectional sets with the uncertainty perturbations are only used by PARCS.

Once the 146 simulations, with the corresponding perturbations, are performed, nonparametric statistical methods are applied for studying the influence of the uncertainty on the macroscopic neutronic information (*postrun* process). Moreover, the selected output model variables for the TABLE 2: Values of β_{eff} and ejected control rod reactivity worth.

Case	$eta_{ m eff}$	Control rod reactivity worth (pcm/\$)	Coords./bank
ARI	0.0052775	1057.8/2.0043581	14-10/5

TABLE 3: Sequence of the events during the simulated transient.

Time	Event
0 s	Start of simulation
2.0 s	The control rod with maximum reactivity worth begins to withdraw
2.1 s	The control rod with maximum reactivity worth is fully extracted
500 s	End of simulation



FIGURE 2: DAKOTA-Jaguar followed methodology.

uncertainty and sensitivity analysis are reactor power, total reactivity, and enthalpy. During the postrun process, the prerun input files generated by Jaguar and the perturbation matrix file are used. However, the matrix has to be modified by adding an extra column which includes the required information for the performed sensitivity analysis. Figure 2 summarizes the followed procedure using DAKOTA-Jaguar computer package.

The modification of the matrix is one of the main parts of the sensitivity analysis and it can be performed following two different approaches. The first one is based on maximum values so the extra column contains the maximum value for each output variable (power, enthalpy, or reactivity) for a given case. The second approach is based on the time step values and it has been repeated three times, one for each output variable. The extra column contains the desired output variable value for each time step for a given case. Furthermore, for this second approach, some interpolations may be required since not all the simulations have the same time steps.

This paper describes the two approaches and the sensitivity analysis performed based on them. Henceforth, the first approach will be named as scalar sensitivity analysis and the second approach as index-dependent sensitivity analysis.



FIGURE 3: SNAP representation of the RELAP5 model.

4. Model Description

The reactor core contains 157 fuel elements. Each fuel element has 264 fuel rods, 24 guide tubes, and 1 tube for the instrumentation. Therefore, the core has been modelled with 157 thermalhydraulic flow channels, with a one-to-one correspondence with the fuel elements. The initial Hot zero power (HZP) steady-state conditions are: temperature equals to 565.58 K, initial density of 740.74 kg/m³, and a total inlet mass flow rate through the core of 13301 kg/s which is distributed among all the channels depending on the cross-sectional area. The transient is started by the ejection of a control rod with the maximum reactivity worth.

RELAP5 is the selected system code for modelling the 157 thermalhydraulic channels, which are connected with branches (*BRANCH*), and the by-pass which is modelled as an independent channel (see Figure 3). The inlet and the outlet boundary conditions are modelled as a time-dependent volume (*TMDPVOL*) and a time-dependent junction (*TMDPJUN*) respectively, as shown in Figure 3.

Radially, the core is divided into $21.504 \text{ cm} \times 21.504 \text{ cm}$ cells (with a one-to-one correspondence between the cells and the fuel assemblies) plus a radial reflector. In total, there are 157 fuel assemblies plus 64 reflector assemblies. Axially, the core is divided into 26 layers (24 fuel layers plus top and bottom reflector) with a height of 15.24 cm each. The total active core height is 365.76 cm.

The neutronic nodal discretization consists of 157×24 active nodes. In addition, 13 different types of fuel elements (including one to represent the reflector), with 291 different neutronic compositions, are considered. The

-0.6

-0.8

- 1

Enthalpy

Diff1

Diff2

SigR1

Siga1



0

0

FIGURE 4: Control rod banks configuration.

neutronic model uses two prompt and six delayed neutron groups. Moreover, zero-flux at the outer reflector surface is considered as boundary conditions for the neutron diffusion equation and the decay heat model is activated.

The control rods are grouped in 6 banks which initially all are fully inserted. In a REA simulation, one of the main parameters that needs to be determined is the control rod with the maximum reactivity worth. Table 2 shows the coordinates and bank which correspond to the maximum reactivity worth control rod. Those results have been obtained using SIMULATE3.

As seen in Table 2, the control rod with the maximum reactivity worth corresponds to bank 5 at the location 14–10. It means that this is the selected rod for being ejected during the transient. Figure 4 represents the control rod banks and the ejected rod, the selected bank is renamed as bank 7.

The transient is started by the ejection of the rod 14–10 which is fully extracted in 0.1 s. The transient is simulated following the sequence of the events showed in Table 3.

5. Results

Recalling what was discussed previously, the sample size which guarantees double tolerance limits with a 95% of uncertainty and with 95% of statistical confidence for the output variables is equal to 146. The uncertainty and sensitivity analysis is performed assuming uniform distribution, on one hand, and normal distribution with three different deviations (0.1%, 0.5%, and 1%) on the other hand. Both cases have been simulated using Random and LHS sampling methods.

5.1. Scalar Sensitivity Analysis. Figures 5 and 6 represent the Partial rank correlation coefficients for the analysed case. From the point of view of the sensitivity analysis, the scalar sensitivity for the maximum power, enthalpy, and reactivity shows that the fast diffusion coefficient (1), the scattering cross-section (3), and both neutrons per fission multiplied by fission cross-section (6 and 7) have the highest influence on the uncertainties for all output variables. Moreover, the influence of absorption cross-sections and thermal diffusion coefficient could be neglected. Those extracted conclusions can be extended to all the cases performed.



Power

Siga2

NuSigF1

NuSigF2

Reactivity

FIGURE 5: Partial rank correlation coefficient for maximum power, maximum enthalpy, and maximum reactivity for LHS normal 0.1% case (1: *Diff1*, 2: *Diff2*, 3: *SigR1*, 4: *Siga1*, 5: *Siga2*, 6: *NuSigF1*, 7: *NuSigF2*).

For simplicity, it has been only presented the comparison between the sampling methods for the normal PDF. In case of uniform PDF, the results are similar to normal PDF but with partial rank correlation slightly increased, that is, all output parameters are more sensitive with respect to input variables uncertainty. In next figures, it is seen that the fast absorption cross-section (*Siga1*) is positive for LHS method (Figure 5) and negative for the random method (Figure 6). Considering the sample size used (146) and the proximity of the mentioned cross-section, the sign change could be due to statistical fluctuations.

Figure 7 shows the scalar sensitivity analysis for the scattering cross-section (SigR1). It is shown that the use of the Uniform PDF to quantify the uncertainty of the input variables increases the sensitivity of a given output variable with respect to a specific input variable. The partial correlation coefficient statistically quantifies the influence of one variable, removing the effect of the rest, and, in this case, Figure 7 shows that assigning equal probability to the range of uncertainty of the variable (uniform distribution) increases the correlation coefficient, since the sampling results in a wider variation across the range compare to a normal PDF. Thus, Figure 7 shows that when normal PDF with LHS is used, the influence of the scattering cross-section is almost constant despite of the dispersion on the normal PDF, since the sampling variation tends to be concentrated around the mean of the normal distribution. Conversely, for Random sampling method, it is shown an increasing trend with the increase of the perturbation deviation. The same trends can be seen on other cross-sectional parameters.

5.2. Index-Dependent Sensitivity Analysis. The indexdependent sensitivity analysis for normal PDF and the two sampling methods are presented in this subsection. For the



FIGURE 6: Partial rank correlation coefficient for maximum power, maximum enthalpy, and maximum reactivity for random normal 0.1% case (1: *Diff1*, 2: *Diff2*, 3: *SigR1*, 4: *Siga1*, 5: *Siga2*, 6: *NuSigF1*, 7: *NuSigF2*).



FIGURE 7: Scalar sensitivity of the scattering cross-section for all simulated cases.

particular case in which the number of runs is equal to 146, critical values for Spearman's coefficient are $r_s = \pm 0.16$; whether the correlation exceeds these values, then the parameter is influential.

First the results of Partial rank correlation coefficient (PRCC) for the output variable Power are presented. As shown in Figures 8 and 9, the most sensitive parameter is the fast diffusion coefficient (*Diff1*) with mostly a strong positive influence on the power. This is followed by the fast fission (*NuSigF1*), the scattering (*SigR1*), and the thermal fission (*NuSigF2*) cross-section, all of them with a similar absolute influence. The difference lies on the positive influence of



FIGURE 8: Partial rank correlation coefficient for LHS normal 0.1%, output variable : Power.



FIGURE 9: Partial rank correlation coefficient random normal 0.1%, output variable : power.

NuSigF1 on the power and negative influence of the other two cross-sections.

As seen, there are changes in the sensitivities of these four neutronic parameters once the insertion of positive reactivity has occurred. Also, the sensitivities change slightly to reach stability when the rods have already been extracted leading to their final value, corresponding to the sensitivity of those values for the reached steady state. All these results and conclusions can be extended to the random sampling normal distribution with 0.1% deviation case as seen in Figure 9. The results for the uniform distribution are similar for those obtained for the normal PDF with 0.1% deviation.

Figure 10 shows the results for normal distribution with 0.5% deviation and LHS sample method. The most sensitive parameters remain unchanged. Furthermore, the values are smoother than in the 0.1% standard deviation case. The



FIGURE 10: Partial Rank Correlation Coefficient LHS Normal 0.5%, output variable : Power.



FIGURE 11: Partial rank correlation coefficient LHS normal 0.1%, output variable : enthalpy.

results for the 1% deviation cases are not shown in this paper because of their similarity to the 0.5% deviation results.

In Figure 11, results of PRC coefficient for the output variable enthalpy are presented. Since these results have few abrupt changes, and for the sake of simplicity, a zoom in time axis has been performed. The extracted conclusions are similar to those obtained for the power. The most sensitive parameters are as shown for the power case. Increasing the deviation, the results are smoother. Using uniform distribution, the input parameters become more sensitive.

In Figure 12, results of PRC coefficient for the output variable reactivity are presented. Again, the same conclusions



FIGURE 12: Partial rank correlation coefficient LHS normal 0.5%, output variable : reactivity.



FIGURE 13: PRC coefficient related to the reactivity and the reactivities.

can be withdrawn, and the most sensitive parameters have the same sign as in the power case.

A final comment is needed with respect to the PRC coefficient variations. All output variables show an abrupt variation in PRC values at time 2 and around 25 seconds. As expected, the variation at time 2 s is due to the rod



FIGURE 14: Power upper tolerance limit (UTL) for LHS sampling method.



FIGURE 15: Enthalpy upper tolerance limit (UTL) for LHS sampling method.

ejection, this variation expands its effect until time 6 s, and then a plateau is reached. The variation at time 25 s could be explained as follows: the PRC is a relative magnitude, so when all input variables are almost constant, a small variation in a thermalhydraulic or neutronic variable could produce an important relative change in the PRC.

The effect of the rod ejection and the reactivity variation are explained in Figure 13. This figure depicts the total reactivity and its decomposed contributions (Doppler, moderator density and control rod reactivities). As expected,



FIGURE 16: Reactivity upper tolerance limit (UTL) for LHS sampling method.

the rod ejection at time 2 seconds implies a fast positive reactivity insertion which is immediately compensated by the Doppler effect (broadening of absorption cross-sections) and a decrease in the moderator (liquid and gas) density. Following the rod ejection, the moderator density reactivity contributes the most to the total reactivity (as negative reactivity).

Figure 13 also shows the PRC coefficient related to the reactivity and the reactivities themselves. It can be seen that fast diffusion coefficient gains influence just after the rod ejection (2 s) and before the insertion of positive reactivity (2.1 s). This phenomenon is due to the loss of the neutron isotropic distribution inside the reactor. Fast diffusion factor maintains its importance (in absolute value). The reason for the change of the fast diffusion sign is the alteration in neutron production due to moderator density and fuel temperature variation (power increase and Doppler effect).

When Doppler reactivity becomes important (2.15 s), absorption parameters increase their influences and fission parameters have opposite tendency. This effect could be explained as follows: the power increases as a consequence of the rod ejection, then the fuel and moderator temperature rise. This is followed by a reduction in moderator density, hence, moderation, and the multiplication factor decrease.

5.3. Uncertainty Analysis. From the point of view of the uncertainty analysis, the results demonstrate that deviations about 0.1% have the smallest influence on the output variables of interest as expected. Figure 14 shows that both LHS and random samplings with normal distribution of 0.1% standard deviation reach a similar peak power at the approximate same time. As a result of the increasing of the uncertainty, there is a slight rise in the maximum output value. However, there is a spread in the time at which the

peak power (and enthalpy and reactivity, see Figures 15 and 16) occurs. Moreover, the intervals of tolerance are greater in normal than in Uniform distributions, so the use of normal PDF provides more conservative results than uniform PDF.

Finally, similar conclusions can be extracted for the uncertainty in power, enthalpy, and reactivity for Random sampling method.

6. Concluding Remarks

This paper has described a Rod Ejection Accident (REA) simulated using the coupled code RELAP5/PARCSv2.7 with a perturbation on the cross-sectional sets in order to determine the response of the computational system to uncertainties in the macroscopic neutronic information.

For all cases, the most influential uncertainties obtained by the scalar sensitivity analysis were the fast diffusion coefficient (1) with a positive influence on power, the scattering cross section (3) and both fission cross-sections (6 and 7) with mixed positive/negative influence. The absorption cross-sections together with the thermal diffusion coefficient could be neglected regarding the influence for the selected output variables. Therefore, the performed sensitivity analyses have shown that the influence of the uncertainties is not dependent on the selected sampling method.

The index-dependent sensitivity analysis showed the same influence for the different neutronic parameters. Moreover, there were sign changes in the most important neutronic parameters which are produced once the insertion of negative reactivity has been occurred. However, in all cases the tendency is to reach a steady-state condition for "long" time simulations. Regarding the sampling methods used, there were no significant differences. Furthermore, deviations greater than 0.1% showed smoother behavior; however, perturbations with standard deviations greater than 1% could lead to a run failure due to the high heat flux generation and consequently properties can be overpassed in steam tables.

Conflict of Interests

The authors of this paper have no conflict of interests to declare.

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